Hyperspectral imaging for bottom type classification and water depth determination

Nikole L. Wilson

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Hyperspectral Imaging for Bottom Type Classification and Water Depth Determination

Nikole L. Wilson


A thesis submitted in partial fulfillment of the requirements for the degree of Masters of Science in the Chester F. Carlson Center for Imaging Science of the College of Science Rochester Institute of Technology

August 2000

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Date 9/12/2000
Hyperspectral Imaging for Bottom Type Classification and Water Depth Determination

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12 SEP 00
The M.S. Degree of Nikole L. Wilson has been examined and approved by the thesis committee as satisfactory for the thesis requirement for the Master of Science degree in Imaging Science.
Abstract

Many recreational, military, and commercial activities take place in shallow coastal waters; therefore, interest is high in characterizing these areas. A variety of methods have been employed to determine water depths and classify the bottom using remote sensing. This research proposes to apply Philpot's principal components algorithm for bathymetric mapping to a MISI hyperspectral image, whereas previously this approach has been used on synthetic data. A description of the principal components algorithm is presented along with an outline of how it was applied to airborne hyperspectral images. The algorithm takes advantage of the ability to implement a deep-water correction, and in this linearized space, perform an eigenvector analysis to determine maximum variance in the data, which is related to depth. Unsupervised classification was performed on the first two principal component scores, resulting in a qualitative depth map and bottom type map.

An extensive water measurement campaign was conducted in Lake Ontario in order to characterize the optical properties of the water at the time the MISI images were taken. These properties were used as inputs to the HydroMod radiative transfer model in order to generate sensor-reaching radiance values for various depths and over different bottom types characteristic of a test site on the central New York shore of Lake Ontario. A principal components regression was performed using the algorithm-processed HydroMod model radiances and image data in an effort to determine the inputs to the image, i.e. depth and bottom type, without having a priori information. The limitations of the algorithm as well as the regression approach are discussed.
Acknowledgments

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Chapter 1

Introduction

An advantage of remote sensing is that it provides a synoptic view and can help reduce the amount of time and money spent on sampling. A drawback is that the intervening atmosphere presents a challenge to the interpretation of remotely sensed images. Remote sensing over water is a particularly difficult task because the water is an additional attenuation source. Various components in the water act as absorbing and scattering centers for the radiation that penetrates into the water column.

Much of the research that has been conducted on remote sensing over water has been concerned with the oceans. Remote sensing over shallow water adds one more complexity to the problem: reflection from the bottom. The radiance reaching the sensor over optically shallow water includes not only radiation reflected from the atmosphere, but also radiation reflected from the surface of the water, from the water column itself, and from the bottom.

Understanding the properties of shallow water is important because many recreational and economic activities take place near shore. Remote sensing is a tool that can be used to understand these shallow water properties, such as bottom type variation and depth. For example, Monroe County is interested in the location and distribution of green algae on the bottom of Lake Ontario, particularly the Ontario Beach area near
Rochester, NY. The Monroe County Environmental Health Laboratory's "1998 Ontario Beach Monitoring Report" states that decaying algal plant matter, specifically cladophora and spyrogyra, was responsible for 13% of the beach closures. These algae wash up on shore where they act as a substrate for bacterial growth and provide to the bacteria a shield from the harmful effects of ultraviolet light. In coastal waters there is a relationship between high levels of bacteria known as indicator bacteria, which are typically found in the presence of harmful bacteria, and the occurrences of swimming-related illnesses. The Health Lab is interested in knowing where the algae are growing in the water as part of their effort to manage the problem. A bottom type map, produced from remotely sensed data, would be useful in addressing such ongoing environmental problems. The algae grow on hard surfaces, such as the rock comprising parts of the lake floor near the Ontario Beach area. The rock and algae reflect light reaching the bottom of the lake differently than the surrounding sand, which is the reason bottom type mapping is capable of distinguishing between a rock bottom and a sand bottom.

In addition to providing bottom type information for applications such as the one discussed above, remote sensing of shallow waters can also provide depth information. Photogrammetric analysis of the bottom of Tampa Bay provided information about circulation patterns in the bay which was extremely beneficial in the evaluation of plans for dredging the bay (Rosenshein et al. 1977). However, interpretation of aerial photographs using photogrammetry is limited because water depth variations are not easily distinguishable from bottom type differences. Remote sensing over shallow waters
calls for a technique which will distinguish the variation in bottom type reflectance from the variation in the reflectance spectra due to absorption and scattering within the water column. This is the problem addressed in the current research.

This research contributes in three ways to the study of using remotely sensed imagery to gain information about depth and bottom type in shallow, coastal water. First, the algorithm used here was implemented on a hyperspectral image taken by the Modular Imaging Spectrometer Instrument (MISI), rather than a synthetic data set. This involved identifying the challenges of using real data, working around them, and analyzing the algorithm's limitations. The algorithm was implemented to determine qualitative depth and bottom type information from images taken at the Ginna power plant and near Ontario Beach. Second, the research shows the usefulness of the bottom classification map to the County Health Lab in their management efforts to prevent beach closures due to algae washing up on the shore. The third contribution is taking Philpot's algorithm in a new direction by using principal components regression (PCR) to quantitatively determine the unknowns (depth, bottom type, water type) that combine to form an image over shallow water. This study illustrates how the radiative transfer model HydroMod can be used as a model to simulate the conditions under which the Lake Ontario MISI images were taken, calculating sensor-reaching radiances, which were then used to calibrate the PCR.
Chapter 2

Background-Literature Review

2.1 Radiance Reaching the Sensor

Remote sensing over shallow water is difficult because of the various components that contribute to the radiance that reaches the sensor. There are essentially two components that make up the sensor reaching radiance. The first is the upwelled radiance scattered from the atmosphere (blue arrow in Fig. 2.1). The second is the radiance reflected from the scene, composed of three different parts: (1) The radiance reflected from the surface of the water (green arrow in Fig. 2.1), (2) water column reflected radiance (violet line in Fig 2.1), and (3) bottom-reflected (orange arrow in Fig 2.1).

Figure 2.1 Components of Sensor-Reaching Radiance
The radiative transfer model, HydroMod, can be used to understand the components shown in Fig. 2.1. HydroMod is a tool for calculating radiance distributions using realistic environmental conditions. It uses the Air Force Laboratory’s MODTRAN (Berk 1989), one of the most accurate radiative transfer computer models available, to calculate the atmospheric conditions through which photons travel on their path toward the water surface and again on their return to the sensor (Fairbanks 1999).

The HydroMod program consists of four modules (Fairbanks 1999). The first module calculates the input radiance distribution using MODTRAN to calculate atmospheric conditions. The second module involves the transition through the water surface both into and out of the water. The third module handles the propagation and reflection underwater. This is accomplished using Dr. Mobley’s Hydrolight code (Mobley 1995, 1996) to solve the radiative transfer under the water. Finally, the light is propagated back through the atmosphere to the sensor using MODTRAN.

**2.1.1 Atmospheric Attenuation**

The radiance reaching the sensor over water first passes through the atmosphere where some of it is scattered and some of it is absorbed. Direct solar radiation is scattered and absorbed, but still proceeds from the general direction of the sun, as opposed to diffuse sky radiation, which results from scattering by aerosols and air molecules. Bukata, et al. (1995) define the atmospheric attenuation coefficient, \( c_s(\lambda) \), as the fraction of radiant energy removed per unit distance due to absorption and scattering as a beam of solar radiation travels through the atmosphere. \( c_s(\lambda) \) is expressed as a
summation of the attenuation coefficients due to the various components that comprise
the atmosphere. Attenuation by the atmosphere is a result of molecular (Rayleigh)
scattering, aerosol scattering, and absorption by gases.

The atmosphere interferes with the signal from the water, requiring that its effect be
removed in order to analyze the scene. The algorithm implemented here on MISI images
subtracts off the effect of the atmosphere, based on the assumption that the atmosphere is
invariant over the scene, in a procedure termed the “deep-water correction”. The
radiative transfer model, HydroMod, was used to model the conditions under which the
MISI images were taken, resulting in sensor-reaching radiance values.

2.1.2 The Air-Water Interface

Photons not scattered by the atmosphere interact with the water surface. At the
surface, they are either reflected, refracted, or transmitted.

Refraction of the light is governed by Snell’s Law,

\[ n_a \sin \theta_a = n_w \sin \theta_w \]

(2.1)
in which \(a\) and \(w\) refer to air and water, respectively, and \(n\) is the index of refraction. The
angle, \(\theta\), is the angle between the direction of the photon flux and the in-water normal.

The reflected photon flux is given by Fresnel’s reflectance formula. For
perpendicular polarized light, the reflectance is
\[ P_\parallel = \frac{\tan^2(\theta_i - \theta_r)}{\tan^2(\theta_i + \theta_r)} \]  
\hspace{1cm} (2.2)

For parallel polarized light, the reflectance is

\[ P_\perp = \frac{\sin^2(\theta_i - \theta_r)}{\sin^2(\theta_i + \theta_r)} \]  
\hspace{1cm} (2.3)

And for randomly polarized light,

\[ \rho = 0.5 \frac{\sin^2(\theta_i - \theta_r)}{\sin^2(\theta_i + \theta_r)} + 0.5 \frac{\tan^2(\theta_i - \theta_r)}{\tan^2(\theta_i + \theta_r)} \]  
\hspace{1cm} (2.4)

Further information on the air-water interface, including the impact of waves, is given in Bukata (1995) and Mobley (1994).

\subsection*{2.1.3 In The Water}

As discussed, the atmospheric and water surface interactions are accounted for in HydroMod (Fairbanks 1999). HydroMod also accounts for the in-water interactions, but the water properties are required. The ground truth gathered for this project allows the optical properties of the water to be determined and used as inputs to HydroMod. The following discussion focuses on the in-water interactions.
Case 1 waters are those waters that have a high concentration of phytoplankton compared to colored dissolved organic matter and nonbiogenic particles or where the phytoplankton covary with the other components. Most coastal water is considered Case 2 water because inorganic or colored dissolved organic matter from land drainage are important and may not covary with absorption by pigments, such as chlorophyll (Mobley 1994). This research is concerned with these coastal waters. The concentrations of these components determine the optical properties of the water.

There are two different categories of optical properties – apparent and inherent. According to Mobley (1994), apparent optical properties are those properties of the water that depend on both the medium and the structure of the light field, and that are regular enough to provide a good description of the water. Inherent optical properties are those properties that depend solely on the medium.

2.1.3.1 Inherent Optical Properties

The inherent optical properties of water include the absorption coefficient $a(\lambda)$, the total attenuation coefficient $c(\lambda)$, the scattering coefficient $b(\lambda)$, the forwardscattering probability $F(\lambda)$, the backscattering probability $B(\lambda)$, the scattering albedo $\omega_b(\lambda)$, and the volume scattering function $\beta(\theta)$ (Bukata 1995). Definitions of these properties are taken from Mobley (1994). Figure 2.2 shows the geometry which will be important in defining optical properties.
Mobley defines a small volume $\Delta V$ of water, of thickness $\Delta r$, which is illuminated by a narrow collimated beam of monochromatic light $\Phi_i(\lambda)$, W nm$^{-1}$. Part of this incident power is absorbed by the water volume and is designated $\Phi_a(\lambda)$. Also, some part of this power is scattered out of the incident beam at angle $\psi$, and is termed $\Phi_s(\psi; \lambda)$. The power in the beam that has not been either scattered or absorbed is transmitted $\Phi_t(\lambda)$ through the volume of water. Assuming that no inelastic scattering occurs and the photons retain their original wavelengths, under the conservation of energy,

$$\Phi_i(\lambda) = \Phi_a(\lambda) + \Phi_s(\psi; \lambda) + \Phi_t(\lambda)$$  \hspace{1cm} (2.5)$$

The spectral absorbance, $A(\lambda)$, is that fraction of incident power that is absorbed within the volume defined above. Likewise, the spectral scatterance, $B(\lambda)$, is that fraction which is scattered. Finally, the spectral transmittance, $T(\lambda)$, is the remainder of the incident
power, which is transmitted through the volume. These three quantities are mathematically defined below:

\[
A(\lambda) \equiv \frac{\Phi_0(\lambda)}{\Phi_i(\lambda)} \quad B(\lambda) \equiv \frac{\Phi_s(\lambda)}{\Phi_i(\lambda)} \quad T(\lambda) \equiv \frac{\Phi_t(\lambda)}{\Phi_i(\lambda)}
\]  

(2.6) (2.7) (2.8)

The inherent optical properties are the spectral absorption coefficient and the spectral scattering coefficient, which are the absorptance and scatterance per unit distance. The spectral absorption coefficient is

\[
a(\lambda) \equiv \lim_{\Delta r \to 0} \frac{A(\lambda)}{\Delta r} \quad (m^{-1})
\]

(2.9)

The spectral scattering coefficient is defined as

\[
b(\lambda) \equiv \lim_{\Delta r \to 0} \frac{B(\lambda)}{\Delta r} \quad (m^{-1})
\]

(2.10)

The total beam attenuation coefficient is the summation of the absorption and scattering coefficients,

\[
c(\lambda) \equiv a(\lambda) + b(\lambda) \quad (m^{-1})
\]

(2.11)

The above terms describe the attenuation of light propagating through water. The remaining inherent optical properties describe the directionality of the scattering interactions. Not only does the amount of power scattered need to be considered, but also
the angular distribution of this scatter: the angular scatterance per unit distance and unit solid angle, known as the spectral volume scattering function is given by

$$\beta(\psi; \lambda) = \lim_{\Delta r \to 0} \lim_{\Delta r \to 0} \frac{B(\psi; \lambda)}{\Delta r \Delta \Omega} = \lim_{\Delta r \to 0} \lim_{\Delta r \to 0} \frac{\Phi_s(\psi; \lambda)}{\Phi(\lambda) \Delta r \Delta \Omega} \quad (m^{-1}sr^{-1})$$

(2.12)

where $\Delta \Omega$ is a given solid angle. The spectral power scattered into this given solid angle is equal to the spectral radiant intensity scattered into the direction indicated by $\psi$ times the given solid angle. Therefore,

$$\beta(\psi; \lambda) = \lim_{\Delta V \to 0} \frac{I_s(\psi; \lambda)}{E_s(\lambda) \Delta V}$$

(2.13)

which gives rise to the definition that the spectral volume scattering function is the scattered intensity per unit incident irradiance per unit volume of water. Irradiance ($E$) is defined as the rate at which the radiant flux, or power, is delivered to a surface. The radiant intensity ($I$) describes the directional information about the flux (Schott 1997).

The relationship between the spectral volume scattering function and the scattering coefficient is defined in the following formula where $\Xi$ represents the unit sphere.

$$b(\lambda) = \int_{\Xi} \beta(\psi; \lambda) d\Omega = 2\pi \int_0^\pi \beta(\psi; \lambda) \sin \psi d\psi$$

(2.14)
The integration defined above is typically divided into forward scattering, over the angles $0 \leq \Psi \leq \pi/2$ and backward scattering over the angles $\pi/2 \leq \Psi \leq \pi$. The forwardscattering coefficient, $b_F$, and the backscattering coefficient, $b_B$, are defined as follows:

$$b_F = 2\pi \int_0^{\pi/2} \beta(\Psi) \sin \Psi d\Psi$$

$$b_B = 2\pi \int_{\pi/2}^{\pi} \beta(\Psi) \sin \Psi d\Psi$$

(2.15) (2.16)

Bukata (1995) explains that the photons scattered into either the forward or backward direction are spoken of in terms of probabilities, or the fractions of the total scattered flux directed into each hemisphere. The forwardscattering probability, $F$, is the ratio of flux scattered into the hemisphere ahead of the incident flux to the total scattered flux. Similarly, the backscattering probability, $B$, is the ratio of the flux scattered into the hemisphere behind the incident flux to the total scattered flux and these probabilities are defined in the following equations.

$$F = \frac{b_F}{b} \quad B = \frac{b_B}{b}$$

(2.17) (2.18)

The last IOP introduced here is the spectral single-scattering albedo, $\omega_0$, which is the probability that a photon will be scattered rather than absorbed, and is defined as
2.1.3.2 **Bulk vs Specific Inherent Optical Properties**

Bulk inherent optical properties (IOPs) are those that are described in the previous section and are based on considering the water column as a whole rather than as various components that absorb and scatter. Specific inherent optical properties are those that are attributed to the individual components in the water that act as absorbing and scattering centers. These specific IOPs are the ones that must be determined when trying to use remote sensing to determine concentrations of the various components in the water. The bulk IOPs, previously defined, are simply summations of the individual specific IOPs.

From Bukata et al. (1995),

\[
\omega_b(\lambda) = \frac{b(\lambda)}{c(\lambda)}
\]

(2.19)

\[
a(\lambda) = \sum_{i=1}^{n} x_i a_i(\lambda)
\]

(2.20)

\[
b(\lambda) = \sum_{i=1}^{n} x_i b_i(\lambda)
\]

(2.21)

\[
B(\lambda)b(\lambda) = \sum_{i=1}^{n} x_i B_i(\lambda)b_i(\lambda)
\]

(2.22)

where

\(B(\lambda)b(\lambda)\) = backscattering coefficient at wavelength \(\lambda\) (product of backscattering probability and the scattering coefficient)

\(x_i\) = concentration of the \(i\)th component of the water column

\(a_i(\lambda)\) = absorption coefficient at wavelength \(\lambda\) for a unit concentration of aquatic component \(i\)
\[ b_i(\lambda) = \text{scattering coefficient at wavelength } \lambda \text{ for a unit concentration of aquatic component } i \]

The specific absorption coefficient and the specific scattering coefficient are frequently referred to as the absorption cross-section and scattering cross-section, respectively. Bukata et al. (1995) states that the governing principle behind the remote sensing of the organic and inorganic components of water is that the optical cross sections provide the link between the concentrations of the individual components in the water and the bulk inherent optical properties. If the concentrations of the individual components in the water can be determined, and the optical cross sections of the water are known, the total attenuation of the light due to absorption and scattering in the water column can be determined.

Bukata et al. (1995) limit their optical model to four components, which are followed in this research. A comprehensive model, which considers the optical cross sections of every aquatic component in natural waters, is unattainable. Their rationale is that for the Great Lakes waters, only a small loss in generality occurs due to using this four-component model, as opposed to a model which includes a fifth component, non-living organics, to account for detrital matter. These non-living suspended organics rarely dominate the color of inland and coastal waters. The four-component model includes pure water (W), chlorophyll (Chl), dissolved organic carbon (DOC), and suspended minerals (SM). Therefore, the bulk IOPs may be defined as follows:
\begin{align*}
a(\lambda) &= a_w(\lambda) + x_1 a_{Chl}(\lambda) + x_2 a_{SM}(\lambda) + x_3 a_{DOC}(\lambda) \\
b(\lambda) &= b_w(\lambda) + x_1 b_{Chl}(\lambda) + x_2 b_{SM}(\lambda) \\
B(\lambda)b(\lambda) &= B_w(\lambda)b_w(\lambda) + x_1 B_{Chl}(\lambda)b_{Chl}(\lambda) + x_2 B_{SM}(\lambda)b_{SM}(\lambda)
\end{align*}

(2.23) (2.24) (2.25)

The coefficients \(x_1, x_2, \) and \(x_3\) are the concentrations of chlorophyll, suspended minerals and DOC, respectively. The absorption cross-section and scattering cross section for Lake Ontario (Bukata 1995) are shown in Figures 2.3 and 2.4. Bukata (1995) makes reference to suspended minerals, but this component will be referred to here as suspended matter because this research does not distinguish the mineral from the organic particles.

Figure 2.3 Pure water absorption coefficient and absorption cross-section spectra for chlorophyll, total suspended mineral, and dissolved organic carbon indigenous to Lake Ontario (Fig 5.5 of Bukata 1995)
In order to generate the sensor-reaching radiances, HydroMod requires the component concentrations for chlorophyll, suspended solids, and DOC. These component concentrations are multiplied by the optical cross-sections of the aquatic components included in the model. Updated optical cross-sections for these components in Lake Ontario, determined from processing and analysis of water samples, are included in the HydroMod model to generate radiance data, with the exception of pure water and chlorophyll. These updated cross-sections are presented in Section 2.2.

2.1.3.3 Apparent Optical Properties

As stated earlier, the apparent optical properties (AOP) depend not only on the medium, but also on the structure of the ambient light field, and they are used whenever a
radiometric quantity other than radiance is used. The first AOP that will be discussed here is the irradiance attenuation coefficient, $K(\lambda, z)$. Bukata et al. (1995) define the irradiance attenuation coefficient as the logarithmic depth derivative of the spectral irradiance at a depth of $z$. The actual definition of $K(\lambda, z)$ results from Beer’s Law (Bukata 1995) and is derived below. A beam of light passing through a medium loses some of its initial radiance flux value, $\Phi_{inc}$, due to absorption loss by an attenuating medium of thickness $\Delta r$, and only $\Phi_{trans}$ remains of the original beam of light, according to the following form of Beer’s law.

$$\Phi_{trans} - \Phi_{inc} = -a\Phi_{inc} \Delta r$$

(2.26)

or

$$\Delta \Phi = -a\Phi_{inc} \Delta r$$

(2.27)

The constant of proportionality, $a$, is defined as the absorption coefficient. Then, in the limit as both $\Delta \Phi$ and $\Delta r$ approach zero, the equation becomes

$$\frac{d\Phi}{\Phi} = -adr$$

(2.28)
which is Beer’s Law. Integrating equation 2.28 from \( r = 0 \) to a distance \( r \) in the absorbing medium, and knowing that the beam coefficient is a function of wavelength yields the following equation:

\[
\Phi(r, \lambda) = \Phi(0, \lambda) e^{-\sigma(\lambda) r}
\]

(2.29)

and consequently for a beam propagating vertically in water,

\[
E(\lambda, z) = E(\lambda, 0 -) \exp[-K(\lambda, z) z]
\]

(2.30)

where \( E(\lambda, z) \) = the value of irradiance at depth \( z \) and \( E(\lambda, 0-) \) = the irradiance just below the air-water interface. Finally, Equation 2.31 defines the irradiance attenuation coefficient, resulting from Beer’s Law being used to describe the attenuation of spectral irradiance with depth \( z \) (Eq. 2.30).

\[
K(\lambda, z) = -\frac{1}{E(\lambda, z)} \left[ \frac{\partial E(\lambda, z)}{\partial z} \right] (m^{-1})
\]

(2.31)

This AOP shows how the irradiance decreases exponentially with depth due to attenuation by the water. The irradiance attenuation coefficient divided into the
downwelling irradiance attenuation coefficient \( K_d(\lambda, z) \) and the upwelling irradiance attenuation coefficient \( K_u(\lambda, z) \) is

\[
K_d(\lambda, z) = -\frac{1}{E_d(\lambda, z)} \left[ \frac{\partial E_d(\lambda, z)}{\partial z} \right] m^{-1}
\]

\[
K_u(\lambda, z) = -\frac{1}{E_u(\lambda, z)} \left[ \frac{\partial E_u(\lambda, z)}{\partial z} \right] m^{-1}
\]

(2.32) (2.33)

where \( E_d \) and \( E_u \) refer to the downwelled and upwelled irradiances, respectively. For a review of these radiometric terms, refer to Schott (1997).

2.2 Composition of Natural Water

Natural waters are composed of a myriad of living, non-living, and once-living material. These components determine the optical properties of the water that were discussed in the previous section

2.2.1 Pure Water

Pure water implies that the water is free from the scattering and absorption effects of organic and inorganic matter. The attenuation due to pure water is due only to water molecules. Pure water typically absorbs weakly in the blue and green regions of the electromagnetic spectrum. As Kirk (1983) states, the absorption of pure water increases above 550 nm and is quite significant in the red. Figure 2.5 shows the absorption and scattering spectra of pure water as measured by Smith and Baker (1981), which are the water optical cross-sections used in HydroMod.
Above 550 nm, the attenuation of light by pure water is dominated by absorption and the total attenuation coefficient due to pure water can be approximated as the absorption coefficient due to pure water. However, in the blue region, $\lambda = 400$-520 nm, scattering by pure water plays a greater role in total attenuation (Bukata 1995). The strong absorption in the red and weak absorption, but strong scattering, in the blue-green region of the spectrum causes the blue appearance of water.

2.2.2 Dissolved Salts and Gases

Dissolved salts and gases are not included in the four-component model discussed earlier. Dissolved salts do affect absorption within the water column, with the most significant effect at ultraviolet wavelengths, $\lambda < 300$ nm. Molecular scattering in mid-oceanic waters due to the pure water/dissolved salt combination is relatively insignificant.
compared to the total attenuation. The specific directional scattering due to pure water/dissolved salts plays a more significant role in molecular scattering. However, for inland waters, the ability of dissolved salts to create a directional nature to $\beta(\psi)$ is significantly reduced compared to mid-oceanic waters due to their much lower concentrations in fresh water (Bukata 1995). Dissolved gases, of which dissolved oxygen is the most significant, also do not produce significant changes to the bulk optical properties of the water, and therefore, are not included in the model.

2.2.3 Dissolved Organic Matter

Dissolved organic matter (DOM) does not have a significant impact on scattering as evidenced by the fact that it is not included in Eq. 2.24. DOM does, however, impact the absorption in natural waters and is often the dominant component in the optical absorption of coastal water (Vodacek et al. 1997). The optically active component of DOM is referred to as Colored Dissolved Organic Matter (CDOM). DOM is a result of excretion, secretion, or decomposition of plants and animals in the water, or of direct input of terrestrial material. Plant or animal materials are transformed into DOM through hydrolysis, photolysis, and bacterial decomposition of their cellular structure. The decomposition of plants and animals results in water soluble humic substances which are responsible for the yellow color observable in some inland and coastal waters. Although these pigments comprise only about 40% of the DOM, the yellow hue has given rise to the various terms given to DOM, such as colored dissolved organic matter (CDOM), yellow substance, gelbstoff, gilvin, etc. (Bukata 1995).
Lake Ontario displays DOM concentrations on the order of 2 g C/m³, which is fairly low compared to average lake water concentrations reported in the literature of 9 or 10 g C/m³. (Bukata 1995) An absorption curve can be represented by the following relationship, which is valid over the wavelengths $\lambda = 350$-700 nm,

$$a_g(\lambda) = a_g(\lambda_0) \exp[-S(\lambda-\lambda_0)]$$

(Bricaud, et al 1981) (2.34)

The subscript, $g$, stands for gelbstoff. The variable, $S$, is a slope parameter assumed to be independent of wavelength. The values for the parameter, $S$ (nm⁻¹), typically range between 0.010 to 0.020, with a mean value of 0.014. The reference wavelength, $\lambda_0$, is typically arbitrary, but usually in the UV or blue. Spectrophotometric analysis of a water sample, filtered to remove scattering particles, with the absorption of pure water, subtracted, becomes an estimate of $a_g(\lambda)$. The study examined the wavelengths between $\lambda = 350$-700 nm because that was the range of the spectrophotometer used. Below $\lambda = 350$-700 nm, there were a few discontinuities in some of the samples measured, but the absorption between $\lambda = 350$ nm and $\lambda = 700$ nm reasonably followed the law shown in Eq.2.34. The normalized CDOM spectral absorption coefficient of Lake Ontario water (Fig. 2.6) used for this study in the HydroMod model was determined from samples collected on May 20, 1999. A spectral absorption coefficient normalized to one at 350 nm is used in the work instead of a cross-section, because DOC measurements were not available. Instead, the normalized
coefficient is multiplied by a scalar to arrive at an appropriate spectral absorption coefficient. The scalar used for Lake Ontario waters was 0.2.

![CDOM Normalized Spectral Absorption Coefficient](image)

Figure 2.6 CDOM normalized spectral absorption coefficient used in HydroMod

### 2.2.4 Suspended Matter

The term “suspended matter” includes both organic and inorganic matter. Suspended matter is derived from plankton, detritus from the decomposition of phytoplankton, zooplankton, and macrophytic plants, as well as terrigenous suspended particles formed by erosion and discharge. A large portion of this suspended matter is suspended minerals, which according to Bukata (1981) have concentrations in Lake Ontario of 0.2-8.9 g/m³. The HydroMod absorption and scattering cross-sections for suspended matter are shown in Fig. 2.7. The absorption cross-section was generated from a curve that represents the average of a set of curves measured from water samples collected on May 20, 1999. The scattering cross-section was taken from a backscattering
cross-section curve measured and modified by Dr. Vodacek to match Bukata’s (1995) curve.

Figure 2.7 Suspended Matter Absorption and Scattering Cross-Sections in HydroMod

In addition, there are various precipitates, a result of chemical activity, that can affect the absorption and scattering within a water body. For example, Landsat first viewed chemical precipitations of calcium carbonate, known as whittings, in the Great Lakes in 1973 (Strong, 1978). As surface waters become saturated with Ca$^{++}$ ions in the summer time, a biological or physical mechanism initiates the whiting.

Zooplankton feed on the algae, detritus, and bacteria, and therefore help to determine the status of the water. For example, a highly productive water body will have a higher concentration of zooplankton, while the populations of zooplankton in natural waters may be patchy because they are moved around by currents, reproductive cycles,
the availability of food, and other factors. The effect of zooplankton on color is largely unknown, but assumed to be minor due to their small concentrations in comparison to phytoplankton and bacterioplankton.

There are also bacterioplankton in the water, which do not contribute to the overall water color, although they probably have some effect on scattering. Planktonic fungi are colorless, chlorophyll-free lower plant forms consisting of cellular filaments containing spores. These planktonic fungi present in the water column are assumed to have negligible optical impact on the optical properties of the water due to their lack of color in addition to their low concentrations (Bukata 1995).

2.2.5 Algal Pigments

Phytoplankton cells contribute to water color, depending on their pigments. All phytoplankton contain chlorophyll and carotenoids, which are responsible for photosynthesis. All green algae contain chlorophyll a, and possibly b and/or c. As Bukata states (1995), the ratio of chl a to chl b is approximately 3:1, and therefore, as Bukata does in his model, the research here focuses on the presence of chl a. Chlorophyll absorption occurs in the blue and red regions of the spectrum (Fig. 2.8), and is more intense in the blue region for chl a.
Decomposed chlorophyll, in the form of phaeophytin, must be accounted for because it causes a peak shift toward shorter wavelengths in the blue region and a peak shift toward longer wavelengths in the red region. The intensity of the absorption for this chlorophyll derivative is weak compared to the intensities of the absorption bands of chlorophyll, but an estimate of phaeophytin is essential to determining the portion of non-living phytoplankton in the water.

Understanding these properties helps in derivation of algorithms for determining water depth and bottom type information.
2.3 Shallow Water Reflectance

The irradiance just below the surface includes the flux scattered back by the water column itself (i.e., the photons that never reach the bottom) and the flux scattered back from the bottom:

\[ E_u(0) = [E_u(0)]_c + [E_u(0)]_b \]  

(2.35)

where

\[ E_u(0) = \text{the upwelling irradiance just below the surface} \]

\[ [E_u(0)]_c = \text{upwelling irradiance just below the surface due to the water column} \]

\[ [E_u(0)]_b = \text{upwelling irradiance just below the surface due to the bottom} \]

The derivation of the following expression for shallow water reflectance is included in Maritorena et al. (1994), who use some simplifying assumptions in order to derive analytical formulas for shallow water reflectance. In order to estimate the irradiance due to the water column, they model an infinitely thin layer of thickness \( dz \) at depth \( z \), where the downwelling irradiance at this point is \( E_d(z) \). The backscattering coefficient for this downwelling light is \( b_{bd} \). Then, the upwelling irradiance created by this infinitely thin layer of water is

\[ dE_u(z) = b_{bd} E_d(z) dz \]  

(2.36)

The irradiance at depth \( z \) can then be expressed as
\[ E_d(z) = E_d(0) \exp(-K_d z) \] (2.37)

where \( E_d(0) \) is the downwelling irradiance at zero depth and \( K_d \) is the downwelling irradiance attenuation coefficient. The upwelling irradiance is also attenuated; this attenuation is expressed by \( -\kappa z \), where \( \kappa \) is the vertical attenuation coefficient of the flux scattered upward from the thin layer of water. According to Kirk (1989), this vertical diffuse attenuation coefficient is different from \( K_d \) because the angular distribution of upward-scattering photons biased toward small angles to the horizontal, where the photons get extinguished more quickly. This bias toward small angles is due to the shape of the volume scattering function. Many measurements of \( K_d \) exist, but \( \kappa \) is not directly measurable. In the middle of the euphotic zone, defined as the depth at which the downward irradiance is 10\% of that penetrating the water surface, it is assumed \( \kappa = 2.5K_d \). The contribution, then, of the infinitely thin layer to the upwelling irradiance just below the surface, \( dE_u(z \rightarrow 0) \), is

\[ dE_u(z \rightarrow 0) = b_{bd} E_d(0) \exp[-(K_d + \kappa)z] dz \] (2.38)

One of the assumptions made in this model is that \( b_{bd}, K_d, \) and \( \kappa \) do not depend on depth. Maritorena et al. (1984) derive the reflectance, \( R(0,H) \) below the surface of a homogeneous ocean with a reflecting bottom located at a depth of \( H \), as

\[ R(0, H) = R_\infty + (A - R_\infty) \exp((-K_d + \kappa)H) \] (2.39)
In Eq. 2.39, $A = \text{bottom albedo}$, $R_\infty = \text{reflectance of the infinitely deep ocean}$, $K_d = \text{vertical attenuation for downwelling irradiance}$, and $\kappa = \text{vertical attenuation coefficient of the flux scattered upward from a thin layer of water}$. This equation (2.39) is the same as Philpot's (1989) equation 4 in the paper in which he describes his principal components algorithm, implemented in this research. The above equation is simplified because as mentioned earlier, $\kappa$ is not directly measurable, and is specific for each situation. The following equation is considered by O’Neill and Miller (1989) as the most familiar form for shallow water reflectance.

$$R(0, H) = R_\infty + (A - R_\infty) \exp(-2KH)$$

(2.40)

However, as Maritorena et al. (1994) suggest, the use of $2K_d$ results in an underestimate of the actual attenuation experienced by the albedo difference, $(A-R_\infty)$.

Gordon and Brown (1974) discuss five factors that affect the diffuse reflectance, $R_d$, of a flat homogeneous ocean with a Lambertian bottom: scattering albedo ($\omega_b$), bottom albedo ($A$), total attenuation coefficient ($c$), a parameter that relates to the scattering phase function, and the bottom depth $z_B$, in addition to the incident irradiance distribution. It is possible to determine water depths even out to depths of 20-30 m in good conditions (i.e. clear water) from $R_d$ if the optical properties and the characteristics
of the bottom are known. They found that the bottom can have a large impact on the
diffuse reflectance, especially at small optical depths, $\zeta$, defined here as

$$\zeta(\lambda, z) = \int_0^z K_d(\lambda, z)z$$

(2.41)

where $K_d =$ downwelling irradiance attenuation coefficient over the subsurface depth $z$
The symbol, $\zeta$, refers to optical depth in this section, as in Bukata’s definition, whereas $\zeta$
will be used as a constant in the derivation of the linear multi-band algorithm in Section
2.4.3. According to Bukata (1995), if $K_d$ is the average value of the irradiance
attenuation coefficient over the depth interval, the following holds true:

$$\zeta(\lambda, z) = K_d z$$

(2.42)

In very clear waters, which have a low value of $K_d$ (i.e., low concentrations of both
organic and inorganic materials, and the scattering and absorption is determined primarily
by the water molecules themselves), optical depth can at times equal the actual physical
aquatic depth. More turbid waters have a higher value for $K_d$ and therefore, the optical
depth will be different than the actual physical depth. In highly absorbing waters with a
highly reflective bottom, the scattering due to the bottom will play a large role at small $\zeta$, and a negligible role at large $\zeta$. In highly scattering waters, the bottom scattering
contributes greatly to the reflectance, even at larger optical depths. Therefore, not only
does the diffuse reflectance depend on the depth of the water and the turbidity, it depends
on whether the turbidity is due to scattering or absorption. It is necessary to determine
the optical properties of the water when quantitatively studying bathymetry using
remotely sensed data.

These models for shallow water reflectance will aid in developing methods for
mapping bottom types and water depth using remotely sensed data. Some of these
methods are discussed in the next section.

2.4 Previous Efforts In Bottom Mapping and Bathymetry

Previous efforts have been made to map the bottom of coastal areas and determine
water depths using remotely sensed data. Some of the earliest techniques used
photointerpretation and photogrammetry of black and white photos. A study of the
bottom configuration in Tampa Bay was conducted in 1971 using photogrammetry
(Rosenshein et al. 1977). Photogrammetry is a part of the quantitative analysis of
remotely sensed data, and uses photographic images to measure height, size, and location
of objects (Schott 1997). Photogrammetric analysis of water depths is difficult for a
number of reasons. The apparent water depth must be multiplied by a factor that
accounts for the refractive index at the air-water interface. Waves at the surface
compound the refractive index problem. Also, the location of the cameras can have an
impact on the accuracy of depth estimates (Tewinkel 1963). Some early work with
pulsed laser technology from an airborne platform yielded accurate depths but was
limited by data recording rates and rate of coverage (Hickman and Hogg 1969). Recent efforts involve techniques which take advantage of multispectral images. Methods dating from the 1960s depended on the ability to find a relationship between water depth and reflected radiance, but these methods require that the properties of the water and the bottom reflectance be uniform (Lyzenga 1985). More often than not, the properties were not uniform and therefore, other techniques were developed.

2.4.1 Single Band Reflectance Model

A simple reflectance model (Jerlov 1976) for remotely sensed bathymetry from multispectral images is given by the following equation

\[ L_i = L_{i\infty} + c_i \cdot R_{ai} \cdot \exp(-2k_i \cdot z) \]  

where \( L_i \) is the radiance value in band \( i \), \( L_{i\infty} \) is the average signal over deep water, \( c_i \) is a constant that is a function of several optical parameters, \( R_{ai} \) is the bottom reflectance in band \( i \) over bottom type \( a \), and \( k_i \) is the diffuse attenuation coefficient. In order to solve for water depth, this equation can be inverted to solve for \( z \). The disadvantage of this method is that it assumes that the bottom reflectance is constant over the bottom type, the atmosphere and water surface conditions are invariant, and also that other background optical effects are either uniform or constant over the scene (Clark et al. 1987).
2.4.2 Ratio Method

Using more than one spectral band is more accurate than using a single band in determining water depth, since the single band method does not account for variation in bottom type (Paredes and Spero 1983). The governing equation for determining water depth based on a reflectance model is similar to that of equation (2.43) above, with different notation,

\[ L_i = L_{si} + k_i r_{bi} \exp(-\kappa_i \alpha z) \]  

(2.44)

where

- \( L_i \) = Radiance in band \( i \) at depth \( z \)
- \( L_{si} \) = radiance over deep water
- \( k_i \) = a function of the solar irradiance, the transmittance of the air and water surface, and the refraction at the water surface
- \( r_{bi} \) = bottom reflectance at the location where the depth is \( z \)
- \( \kappa_i \) = effective attenuation coefficient of the water
- \( f \) = accounts for the path length through the water

If spectral bands exist such that the ratio of the bottom reflectance in the bands is constant throughout the scene, an equation independent of depth can be found

\[ (r_{A1})^{C1} (r_{A2})^{C2} = (r_{B1})^{C1} (r_{B2})^{C2} = ... = \alpha \]  

(2.45)

where \( C1, C2 \), and \( \alpha \) are chosen to make the equality of the bottom reflectance ratios true. \( A, B \ldots \) in the above equation represent different bottom types. Assuming that a pair of bands exists such that the ratio of the bottom reflectances in the two bands is the same
for all of the bottom types in the scene, $z$ is solved for as a function of light intensity, valid for all bottom types. Another way to write the assumption is

$$\frac{r_{A1}}{r_{A2}} = \frac{r_{B1}}{r_{B2}} = \ldots = R_b$$

(2.46)

Then, Eq 2.45 can be inverted and solved for depth, according to the following equation

$$z = \frac{1}{(\kappa_1 - \kappa_2)f} \left[ \ln\left( \frac{k_1}{k_2} \right) - \ln\left( \frac{R}{R_b} \right) \right],$$

where

$$R = \frac{(L_1 - L_{v1})}{(L_2 - L_{v2})}$$

(2.47)

The advantage of this technique is that the depth is not affected by a change in bottom type nor a change in water quality if $(\kappa_1 - \kappa_2)$ stays constant. The limitations of this technique are that one must find the wavelengths that satisfy the criterion that the ratio of the bottom reflectances in the two bands is the same, and the criterion that the attenuation coefficient remains constant, which indicates that the depth is insensitive to changes in water quality. A pair of wavelengths may not exist which satisfy these assumptions; therefore, it may not be possible to determine the water depth using this technique (Lyzenga 1978).

A similar ratio method can also be used to classify the bottom composition. This algorithm makes use of the existence of two bands for which the attenuation coefficients
(absorption coefficient plus scattering coefficient), $\alpha$, are the same, which removes the depth dependence from the model in Eq. 2.44, reducing the ratio to

$$R = \left( \frac{k_1 r_{a1}}{k_2 r_{a2}} \right)$$

(2.48)

Lyzenga (1985) cites higher spatial resolution as an advantage of this technique. The disadvantage of the technique is that it requires water depth calibration and is more sensitive to environmental parameters. Using this technique, Wezernak and Lyzenga (1975) mapped the distribution of algae (cladophora) in Lake Ontario in 1972. Equation 2.49 describes the bottom-reflected signal received at the sensor, not including atmospheric effects.

$$V = V_s + k_0 e^{-(\sec \theta + \sec \phi) \alpha z}$$

(2.49)

where

- $V$ = voltage received
- $V_s$ = surface reflectance
- $K$ = constant which incorporates solar irradiance and scanner characteristics
- $\rho$ = bottom reflectance
- $\theta$ = viewing angle (from vertical)
- $\phi$ = solar illumination angle (from vertical)
- $\alpha$ = volume attenuation coefficient (absorption coefficient plus scattering coefficient)
- $z$ = water depth

Lyzenga's approach involves using a ratio of two spectral bands that have similar attenuation coefficients ($\alpha$). In order to do this, the following conditions must be met:
1) the attenuation coefficients in the two spectral bands must be equal or assumed so, and
2) there must be significant contrast between the bottom reflectances of the cladophora and other bottom features in the spectral bands chosen. Therefore, $\alpha_1 = \alpha_2$, and the signals received in the two different channels are then proportional to the bottom reflectance, but independent of depth. Figure 2.9 shows an example of the ratio imagery produced by this method. The dark areas are those occupied by cladophora, as verified by ground truth collected in the nearshore region from 5 transects extending into the lake.

Fig. 2.9 Ratio Imagery, Site 5, North Hamlin Beach (Lyzenga and Wezernak 1975 Figure 4)

This technique is limited to bands for which the attenuation coefficients are equal, which is not true in every situation. There is also a limitation to the materials one can distinguish because the bottom reflectance ratios for the different materials must be different. For example, the method is unable to distinguish between sand and mud bottoms because they have similarly shaped reflectance spectra. Lyzenga (1978) makes a very important point when he indicates that the ratio method worked for the cladophora case because “the vegetation reflectance has distinctive features (due to chlorophyll
absorption) in the blue-green region of the spectrum where the water attenuation is at a minimum."

Although more flexible than the single-band method, these band ratio methods are limited because they only take advantage of two bands.

2.4.3 Other Multispectral Methods

From multispectral data, Lyzenga (1981) derives bottom depth information, which depends on the relationship that the bottom-reflected radiances varies linearly with bottom reflectance and exponentially with depth, according to Equation 2.50 (Lyzenga 1978),

\[
L_i = L_{si} + k_i r_{Bi} \exp(-\kappa_i f z)
\]  
(2.50)

where

- \(L_i\) = measured radiance in band i
- \(L_{si}\) = deep water radiance
- \(k_i\) = a constant which includes the solar irradiance, transmittance of the atmosphere and the water surface, and the reduction of the radiance due to refraction at the water surface
- \(r_{Bi}\) = bottom reflectance
- \(\kappa_i\) = effective attenuation coefficient of the water
- \(f\) = a geometrical factor to account for the pathlength through the water
- \(z\) = water depth

Lyzenga (1978) modifies Eq. 2.50 to include the effects of scattering in the water and internal reflection at the water surface; examination of the model indicates that the scattering term has the same depth dependence as the bottom-reflected radiance.
His algorithm defines a new variable, $X_i$, that varies linearly with depth,

$$X_i = \ln(L_i - L_a)$$

(2.51)

The variables, $X_i$, that result from the above equation are approximately linear functions of depth and are related to each other linearly for the same bottom type. Therefore, if the $X$ variables from two different bands, $X_i$ and $X_j$, are plotted against one another, the points will fall along a straight line, with a slope of $K_i/K_j$ where $K$ is the irradiance attenuation coefficient, which was defined in Section 2.1.3.3. Analysis of the correlation between the variables yields the ratio of the attenuation coefficients in the two wavelength bands used. Figure 2.10 (Lyzenga’s Figure 1b) is an example of the linearized space where bands 5 and 7 are plotted against one another (Lyzenga 1981).

![Figure 2.10 Scatter plot of X-values for aircraft bands C5 and C7](image-url)
When the bottom reflectance changes, the data will fall along a parallel line which is displaced from the first line. Another variable, \( Y \), can be defined which measures the amount of this displacement between the lines, given by

\[
Y_i = \frac{K_i \ln(L_i - L_u) - K_i \ln(L_j - L_u)}{\sqrt{K_i^2 - K_j^2}}
\]

(2.52)

by geometric reasoning, where \( K_i \) is the irradiance attenuation coefficient of the water in band \( i \). \( Y_i \) is independent of water depth and is related to the bottom reflectance as in Eq. 2.53, assuming that the bottom-reflected radiance \( (L_i - L_u) \) is proportional to the bottom reflectance and varies exponentially with water depth according to

\[
Y_i = Y_{i0} - \frac{K_i \ln r_i - K_i \ln r_j}{\sqrt{K_i^2 - K_j^2}}
\]

(2.53)

where \( r_i \) is the bottom reflectance in band \( i \) and \( Y_{i0} \) is a constant for fixed illumination and atmospheric conditions.

The variable \( Y \) then acts as a depth-invariant index for the bottom type. This algorithm depends on having a priori knowledge of the attenuation coefficients. To use this technique, an area of uniform bottom type must be selected, which requires knowledge about the scene. One method for determining areas of uniform bottom type is
a clustering routine on scatter plots of the data; the higher the uniformity of the bottom, the higher the correlation is between the spectral bands in linearized space, as can be determined by an inspection of the scatter plots. Figure 2.7 is a scatter plot of data over a sand bottom, and shows high correlation between $X_5$ and $X_7$, indicating high uniformity of the bottom type. The ratio of water attenuation coefficients can then be determined by regression.

Lyzenga (1981) applied this algorithm to aircraft and Landsat data of North Cat Cay, Bahamas. His results for the aircraft data were reasonably accurate in mapping bottom reflectance variations without knowledge of the water depth. The Landsat results were not nearly as accurate because only one of the spectral bands could penetrate deep enough into the water, and Landsat has poorer spatial resolution, which makes it more difficult to select an area in which the bottom is uniform.

Another technique for reducing depth dependence defines a variable $Y$,

$$Y_i = \sum_{j=1}^{N} A_j X_j$$

(2.54)

which is obtained by rotating the coordinate system so the $Y_N$ axis is parallel to the direction of changing depth (Lyzenga 1978). If the linear transformation is a pure rotation, $Y_N$ will only be dependent on the water depth assuming this is the primary parameter affecting the brightness, while the remaining variables are functions of the bottom reflectance. Lyzenga states that this is similar to principal component analysis.
only in that it involves a rotation transformation. The transformation removes the depth dependence from all but one variable, and does not necessarily reduce the number of variables. This method is better than the ratio method because it does not require that the wavelength bands have equal water attenuation coefficients or that there are equal bottom reflectance ratios for all bottom types. However, the method is more complex.

Lyzenga (1985) also presents another technique for mapping bathymetry, which is a hybrid of both an active and a passive technique. He makes use of pulsed laser technology by using it to calibrate the passive multispectral data for depth. The advantage of this technique is that it does not rely on sea-truth data for depth calibration. This technique incorporates the laser's accuracy in determining depth with the higher spatial resolution of the multispectral scanner (MSS).

Clark et al. (1987) describe another technique for determining depth, the linear multiband algorithm. This method gives the depth by

\[ z = \sum \omega_i (1/2k_i) \ln(c_i \cdot R_w) - X_i \]

(2.55)

where the symbols are defined above in equation 2.50, \( X_i = \ln(L_i - L_{i0}) \) where \( L_{i0} \) is the average signal over deep water, and the sum is taken over several bands with the constraint that the weights, \( \omega_i \), sum to one (\( \sum \omega_i = 1 \)). The testing of this algorithm involved the use of 600 points of known depth for georeferencing. Three hundred of these points were used in a regression fit of the model equation, while the remaining 300
were used to test the calculated depth against the actual depth. The deep-water signals \( L_{\infty} \) were subtracted from the corresponding \( L_i \) values in order to correct for atmospheric scattering, etc. This linear multiband method builds on the two-band ratio assumption that two bands can be found for which the ratio \( c_1R_{a1}/c_2R_{a2} \) remains constant over different bottom types. The assumption that the ratio \( c_1R_{a1}/c_2R_{a2} \) remains constant is generalized by assuming that there are constants \( \zeta_i \) and \( \alpha \) independent of bottom type \( a \), so

\[
(c \cdot R_{a1}) \zeta_1 \cdot (c_2 \cdot R_{a2}) \zeta_2 \cdot (c_3 \cdot R_{a3}) \zeta_3 K = \alpha
\]

(2.56)

Certain weights can be found so that when used in Eq 2.55, an equation for \( z \) is produced where \( z \) is independent of bottom reflectance, \( R_{a1} \), and depends only on the values \( \zeta_i \):

\[
z = \left( \frac{1}{2} \sum \zeta_i k_i \right) (1 - \zeta_1 X_1 - \zeta_2 X_2 - K)
\]

(2.57)

This equation may be written in a more generalized form. The following equation is for a two-channel model

\[
z = A_0 + A_1 X_1 + A_2 X_2
\]

(2.58)
The coefficients $A_0, A_1, \ldots A_n$ are constants that are independent of the bottom type at which the depth is being calculated. A linear regression is performed on the model equation against the calibration points from which the outputs are the coefficients $A_0, A_1, \ldots$ which can then be used in equation 2.58 to determine depth. The linear multi-band algorithm (Clark et al. 1987) performed better than the band ratio method (Lyzenga 1978) applied to the same data. However, both models underestimated the depth in shallow areas and overestimated the depth in deeper areas. In addition to performing better than the ratio method, the linear multi-band method did not depend on clustering and classification routines to find areas of similar bottom reflectance.

Another method for mapping bottom reflectance and determining depth is found in Bierwirth et al. (1993). The method involves separating the effect of water depth variation from the spectral nature of the substrate. The algorithm derives both substrate reflectance and depth. The algorithm assumes that the water is relatively clear and there are only small variations in the concentrations of water column components. They tested their approach using data from Hamelin Pool, Shark Bay, Western Australia, and therefore, met this assumption because that area is characterized by shallow, clear water. The algorithm applies a constraint, which standardizes the sum of the logarithms of band substrate reflectances. One of the problems with this algorithm is that it derives a value for the attenuation coefficient specifically for Hamelin Pool, Shark Bay, Western Australia. Unless the waters one is working with are similar to these Australian waters, attenuation coefficients would have to be derived from known bathymetric data. The
advantage of this algorithm is that it removes the effect of water depth variation and retains the spectral nature of the substrate.

2.5 Principal Components Method

The principal components algorithm was developed by Dr. William Philpot (1989) and is a generalization of Lyzenga's approach (1978). The benefit of this algorithm is that it extracts depth information and bottom type information even when the conditions are not ideal. Philpot begins with a very simple radiative transfer equation,

\[
L_d = L_b \exp(-gz) + L_w
\]  

(2.59)

\(L_d\) = radiance observed at the remote detector
\(g\) = an effective attenuation coefficient of the water
\(z\) = depth of water column
\(L_b\) = radiance term which is sensitive to bottom reflectance
\(L_w\) = remotely observed radiance over optically deep water

The model assumes that the optical properties of the water are vertically homogeneous. For the shallow waters that are being considered here, this seems to be a reasonable assumption, although the results will show the limitations of the assumption. The coefficient \(g\) is a two way attenuation coefficient and is defined according to

\[
g \approx k_d + aD_u
\]  

(2.60)

where \(k_d\) is the diffuse attenuation coefficient for downwelling light that was defined above, \(a\) is the beam attenuation coefficient, and \(D_u\) is the distribution factor for upwelling irradiance. As discussed in Kirk (1989), the distribution factor for upwelling
irradiance is different from that of the downwelling irradiance since the angular
distribution of the photons scattered upward is biased toward the horizontal. The term \( g \) is approximately equal to the attenuation for downwelling light plus the attenuation for
the upwelling irradiance.

In order to quantitatively solve for depth, \( L_d \), \( L_b \), \( g \) and \( L_w \) must be known. Past
methods (Lyzenga 1978) (Paredes and Spero 1983) (Spitzer and Dirks 1987) have
assumed that some of these terms are constant over the scene. They also assume that the
radiance observed over deep water is constant. Next, they obtain \( L_d \) for two or more
known depths. With a system of two equations and two unknowns, they solve for \( L_b \) and \( g \). Philpot (1989) describes a more complete radiative transfer equation, which includes
atmospheric effects, sea state, water reflectance, and other terms in order to generate a
synthetic data set upon which to implement his algorithm. He demonstrates that his
principal components algorithm works on his synthetic data. The present research
implements the algorithm on an actual scene in order to derive qualitative bottom type
and depth maps.

Philpot describes three cases in his paper. For the purposes of this research, the
case 2 assumptions of variable depth and variable bottom type will be made. Under case
2, \( L_w \) and \( g \) are still assumed to be constant over the scene and the water is assumed to be
vertically homogeneous. A deep-water correction, defined in Eq. 2.61, can be performed
because \( L_w \) is assumed constant. This procedure defines a new variable, \( X \).
\[ X = \ln(L_d - L_w) = \ln(L_b) - gz \quad \text{when } L_d - L_w > 0 \]

and

\[ X = \ln(L_w - L_d) = \ln(-L_b) + gz \quad \text{when } L_d - L_w < 0 \]

(2.61)

Usually, it is assumed that \( L_d - L_w > 0 \) because the bottom reflectance is typically greater than the water reflectance. The ratio methods discussed earlier used a ratio of measurements taken in different spectral bands, which resulted in an improvement in the depth estimate over a single spectral band. It follows that using even more spectral bands will improve the results.

A new variable is defined, \( Y \), according to

\[ Y = a \cdot X = a \cdot \ln(L_b) - (a \cdot g)z \]

(2.62)

\( Y \) = a scalar variable
\( X = \ln(L_d - L_w) \), a linearized measurement vector
\( g \) = an effective spectral attenuation coefficient vector
\( a \) = unit vector of arbitrary coefficients

The components of the vectors represent different spectral bands. When using two bands, Eq. 2.62 is reduced to the band-ratio model when \( a = r = (1, -1) \). Using this method (Eq. 2.62) with the two-band approach discussed above shows that the two band coefficients are not optimal. However, optimal coefficients can be determined using eigenvector analysis, from which the first eigenvector consists of the optimal coefficients for determining depth. This optimal unit vector is referred to as \( a_{opt} \), highlighting its parallel relationship to the direction of changing depth in linearized measurement space.

Fig. 2.8 is a scatter plot from Philpot’s article (1989) of \( X \) at 550 nm vs \( X \) at 650 nm.
which demonstrates how depth varies linearly and how the optimum coefficient vector, $a$, points in the direction of maximum variance.

Figure 2.11 Linearized radiance data for the two-band case. (Philpot 1989 Fig. 1)

Fig. 2.12 shows how much of an improvement the optimal coefficients are over the ratio coefficients ($a = (1,-1)$) when applied to Philpot's (1989) synthetic data.
Figure 2.12 Comparison of noise in predicted depth using simple ratio vs optimal coefficients (Philpot 1989 Fig. 2)

For case 2 situations, the data form separate but parallel clusters in the linearized measurement space $(X_1, X_2)$ in Fig. 2.13. For this reason, adequate difference is required in bottom reflectance between the various bottom types in order to distinguish between clusters. Each of these clusters will be aligned with the optimal coefficient vector, $a_j$. The scalar variable, $Y_{jb}$ defined in Eq. 2.62 will be sensitive to depth for each bottom type if an eigenvector analysis of each bottom type is performed. In order to obtain the absolute depth information, $L_b$ must be known for each bottom. This can be found using the system of two equations in two unknowns, which requires $L_d$ for two known depths over each bottom type.
The clusters in linearized space are separated by a certain distance, which is related to the difference between the bottom reflectances. This separation can be seen in Figure 2.13, a scatter plot (Philpot 1989), in which shows synthetic data for three different bottom types (sand, silt, and vegetated).

![Figure 2.13](image)

Figure 2.13 Linearized radiance data - constant water, but varying depth and bottom type (Philpot 1989 Fig. 3)

A second vector, \( \mathbf{a}_\perp \), is perpendicular to the optimal coefficients vector \( \mathbf{a}_j \) and characterizes \( Y_\perp \), which is independent of depth but sensitive to the bottom type. The vector \( \mathbf{a}_\perp \) is perpendicular to \( \mathbf{a}_\parallel \), which is parallel to \( \mathbf{g} \), so that \( \mathbf{a}_\perp \cdot \mathbf{g} = 0 \). \( Y_\perp \) is a scalar variable independent of depth according to:
showing that the bottom type may be characterized by the scalar variable $Y_\perp$.

Philpot’s (1989) Case 3 includes varying water type in addition to varying depth and bottom type. He indicates that using a single deep-water observation to linearize the entire data set when different water types exist can result in nonlinearities and errors unless the effective attenuation coefficients of the different water types are spectrally proportional. The absolute depth prediction equation determined for one water type may yield incorrect results when applied to another water type. Therefore, $L_b$, $L_w$, and $g$ and the optimal coefficient vector, $a$, would need to be determined for each water type.

Theoretically, these parameters can be estimated if at least three depths are known for each water type, which requires that the depths must be assigned to their respective water types prior to analysis. Another difficulty exists if two pixels representing two different depths and different bottom types are spectrally identical. A preferable method for working with an image containing different bottom types is to partition the image into areas based on water type. Then, the appropriate deep-water pixels can be selected to perform the linearization of the data.

2.6 Choosing the Method

The principal components algorithm (Philpot 1989) described in Section 2.5 was chosen because it seemed the most straightforward to implement. The single band reflectance model (Jerlov 1976) assumes that too many factors are constant – bottom
type, atmosphere, and water surface conditions. The two-band ratio methods yield more accurate results than the single band model. However, the two-band method have other limitations. The ratio methods require that the attenuation coefficients remain constant or that the ratio of the bottom reflectances in the two bands is the same (Paredes and Spero 1983). A pair of wavelengths that satisfy either of these criteria may not exist (Lyzenga 1978). Also, when using a similar ratio method to distinguish between different bottom types, there must be sufficient difference in their reflectances (Lyzenga and Wezernak 1978) in addition to meeting the condition that the attenuation in the two spectral bands must be equal. Additionally, this technique requires water depth calibration and is more sensitive to environmental parameters. Some of the other methods require a priori knowledge or the ability to derive attenuation coefficients that are specific for a particular area (Bierwith et al. 1993). These methods only take advantage of two bands. The attractive feature of the principal components algorithm is that it takes advantage of the numerous bands in a hyperspectral image. The algorithm extracts both depth and bottom type information even when the conditions are not ideal. The other algorithms reviewed looked at either determining water depth or determining bottom type, but not both in the same algorithm. The assumption at the start of the research using Philpot's (1989) algorithm is that the water type is constant. The results will show that this assumption, while not valid over the entire image processed, was more valid over smaller portions of the image, carefully selected to approach the assumption of constant water type.
Chapter 3

Methods

The approach taken in this research involves the use of various methods and tools. An understanding of these methods, to include their strengths and weaknesses, must be understood prior to a discussion of the approach taken.

3.1 Principal Components Analysis

The final method for bottom type classification and water depth determination discussed in Chapter 2 was Philpot’s (1989) principal components algorithm, selected for implementation in this research. Some of the benefits of this algorithm include ease of implementation and capability to take advantage of hyperspectral information in addition to providing both depth and bottom type information. These advantages result from the use of principal components analysis to transform the linearized data ($X'$s) into eigenvectors by finding the variability in the data.

Each pixel of the MISI images, to which the algorithm was applied, contains a spectrum of calibrated radiance values in 63 bands. The variations in the spectra are related to depth, bottom type, water type, and other changing conditions which contribute to the signal in addition to the instrument variations such as detector noise, etc. Yet, there exists some amount of independent variation in the spectral data. The PC method finds the variability in the data. It is the assumption of this research that the largest
variations in the radiance spectra are due to the different input factors, such as depth, bottom type, and water type, especially after linearizing the data (Sec. 2.5). PCA breaks down spectra into their most significant variations, where the variation spectra are known as eigenvectors, or principal components. Eigenvectors are useful in many areas of math and science. The basic eigenvalue equation,

\[ A\nu = \lambda \nu \]

is satisfied for certain \( \lambda \) and \( \nu \), the eigenvalues and eigenvectors. \( A \) is a square (usually symmetric) matrix, and \( \lambda \) is an eigenvalue of \( A \), found by solving the following equation,

\[ \det(A - \lambda I) = 0 \]

where \( I \) is the identity matrix. Once the eigenvalues are found, the eigenvectors can be found.

In order to implement this Principal Components Algorithm, the principal components must be obtained through eigenvector analysis. The eigenvector corresponding to the largest eigenvalue of the covariance matrix indicates the direction of greatest variance. The covariance matrix is defined as
The second-largest eigenvector indicates the direction of greatest variation perpendicular to the first eigenvector. These are the two eigenvectors that are required to implement the principal components algorithm (Philpot 1989). Eigenvectors can be used to predict what the unknown inputs were and are often used in place of the original spectra when doing inverse least squares regression. This procedure of using the principal components in place of the original spectra in regression is called Principal Components Regression (PCR) and is defined in Sec. 3.3.

An advantage of using principal components analysis is that it separates out the factors that are independent of each other, although there is no guarantee that these factors have physical meaning. One limitation of PCA is that there can be problems with collinearity, if the spectra share the same variations, although different in magnitude.

The PC analysis was performed in IDL using a publicly available program called PCA.PRO which is located on the internet at the following website, http://idlastro.gsfc.nasa.gov/contents.html. A copy is located in Appendix B along with the IDL program used to implement Philpot's principal components algorithm on an
image. This program is based on the PCA method in Murtaugh and Heck (1987). The PCA.PRO program standardizes the variables, i.e. it corrects each observation for its mean and standard deviation. Mean centering is important because it enhances the subtle differences between spectra, essentially removing the first most common variation before the data is processed by the PCA algorithm. PCA.PRO also normalizes the eigenvectors by the square root of the eigenvalues.

PCA is used in the algorithm implemented in this research to determine qualitative bottom type and water depth maps. One of the goals of this research was also to determine quantitative depth information without extensive ground truth, using a procedure, principal components regression. PCR combines the benefits of principal components analysis with regression.

3.2 Regression

Regression analysis is a statistical method for predicting values of dependent variables (Y) from a collection of independent variables (X). Regression is used to find the relationship between the Ys and the Xs by estimating the regression coefficients from the regression equation, \( Y = Xb \). For multiple variables, a linear relationship can be assumed in order to form a linear regression, as in the following equation,

\[
Y = b_0 + b_1X_1 + b_2X_2 + \ldots + b_pX_p
\]

(3.5)
where \( p \) = number of observations, \( Y \) = independent variables, \( X \) = dependent variables, and \( b \) = a vector of regression coefficients. The regression coefficients are solved for according to the following equation,

\[
b = X^{-1}Y
\]

(3.6)

An estimate of the inputs (\( \hat{Y} \)) is obtained by plugging \( X \) into the equation, \( \hat{Y} = Xb \) using the regression coefficients, \( b \), found in Eq. 3.6. The regression coefficients are determined such that the sum of squares of error is minimized,

\[
\text{min } \sum \left( y_i - \hat{y}_i \right)^2
\]

(3.7)

The problem with inverse least squares regression is that the number of variables cannot exceed the number of observations due to the dimensions of the matrices. Theoretically, adding additional observations should allow for additional variables; however, the observations tend to decrease and increase together as the constituents of the observation spectra change, known as collinearity. An additional concern while using regression is overfitting, which occurs at the point when adding additional variables no longer increases accuracy, but instead the prediction accuracy gets worse. Combining
regression with the principal components analysis discussed in the previous section yields a procedure called principal components regression.

### 3.3 Principal Components Regression

One of the concerns in implementing Philpot's (1989) principal components algorithm on the MISION images was that the PC algorithm assumes constant water type. An early thought in this research was that quantitative depth and bottom type information could be obtained through PCR because the regression coefficients would be determined from HydroMod model data where water type was varied in known amounts along with depth and water type. Then, depth and bottom type could be determined regardless of varying water type, and the need for extensive ground truth would be eliminated because the regression coefficients are determined from model data.

PCR combines PCA spectral decomposition with the inverse least squares regression method. A spectrum, such as the radiance spectra, which are the expected output of HydroMod, may be represented through PCA by a collection of a series of scores and factors, as in the following figure.
PCA breaks apart the spectral data into the most common spectral variations (eigenvectors) and the corresponding scaling coefficients (scores). For PCR, the regression described in the preceding section was performed not on the X matrix itself, but on the scores matrix, which is determined by multiplying the X matrix times its principal components.

One of the advantages of PCR is that it reduces collinearity in the observed spectral radiances, which is important in this situation because hyperspectral data are almost always highly correlated. When the predictor variables are highly correlated, it is difficult to obtain a good inverse of $X^T X$; as the predictor variables become more correlated, the same thing occurs to the regression coefficients themselves (Jackson 1991). PCR relates the principal component scores to the variables of interest, and hopefully separates the effects of the variables of interest on the spectra. There is no guarantee that the pca vectors directly correspond to the constituents of interest, although
in this research, the assumption is that the first principal components carries depth information and the second carries bottom type information. Another disadvantage of PCR is that generally, a large number of observations are required for accurate calibration, while still being careful to avoid collinearity. The greatest limitation, with regards to this research, is that PCR does not work on categorical data. The implications of this limitation are discussed in Chapter 5.

The regression coefficients were calculated from the scores, a result of eigenvector analysis of the HydroMod radiance outputs. These radiance spectra were generated by the radiative transfer model, HydroMod, for different bottom types, depths, and water types. The water types that served as inputs to HydroMod were determined from processing of water samples collected at the area of study, the Ginna power plant.

3.4 Water Sampling

Extensive water sampling was undertaken at the Ginna power plant and the Ontario Beach area of Lake Ontario, where the Genesee river empties into the lake. The latter field sampling included stations in Braddocks Bay, Irondequoit Bay, and at the Russell power plant. These field sampling efforts were made throughout the summers of 1999 and 2000. The field sampling used as inputs to HydroMod was made at Ginna on September 3, 1999 and Ontario Beach on July 5, 2000. These samplings were made during an overflight of the MISI aircraft and an overpass by one of the following sensors: AVIRIS, Landsat 5, or Landsat 7. At each water sampling location, various measurements were made and water samples were collected. The GPS coordinates were
recorded at each location in addition to collecting a sample of the water near the surface. Also, secchi depths were determined at various locations and where the water was shallow enough, the secchi disk was lowered to the bottom to determine depth.

3.4.1 Filtering

The water samples were filtered on the same day they were collected. They were filtered onto Whatman GF/F 25 mm filters, which is common practice (Mitchell 1990), (Bricaud and Stramski 1990). A pump was used to create a vacuum which forces the water through three different filters: one used for Total Suspended Solids (TSS), one for Chlorophyll a, and one for particle absorption. The volume of water filtered through each filter was recorded in order to calculate component concentrations. The weight of the TSS filters were recorded prior to filtering in order to calculate the difference between the post-filtered weight and the pre-filtered weight. Each of the filters was placed in a plastic capsules which was labeled according to the water sample number and the component concentration being measured. The plastic capsules with the filters intended for chlorophyll extraction were placed in a bag in the freezer to await analysis. The September 3, 1999 filters were stored for 12 days prior to processing for chlorophyll concentration. The tissue prep capsules help protect the filters from light and ice. The Monroe County Environmental Health Laboratory Standard Operating Procedures located in Appendix C states that if the sample is frozen and kept in the dark, it can be held up to 3 weeks (1996). The particle absorption filters were analyzed immediately.
3.4.2 Particle Absorption

The particle absorption was analyzed using a Shimadzu spectrophotometer. A reference filter was prepared by filtering distilled water through the filter. The spectrum of the reference filter was subtracted from the absorption spectrum measured for each of the sample filters, and the resultant spectra were recorded. The particle absorption spectra were corrected for the multiple scattering effects due to the filter using a quadratic fit:

\[ OD_s(\lambda) = aOD_f(\lambda) + b[OD_f(\lambda)]^2 \]

\hspace{1cm} (Mitchell 1990) (3.8)

where \( OD_s(\lambda) \) is the optical density of phytoplankton in suspension, and \( OD_f(\lambda) \) is the optical density of the suspension on a filter. Published coefficients, \( a \) and \( b \), given by Cleveland and Weidemann (1993) are currently used in the particle absorption process utilized by the Digital Imaging and Remote Sensing (DIRS) group. The absorption due to particulates was then calculated using the following equation (Mitchell 1990),

\[ a_p(\lambda) = 2.3OD_s(\lambda)/l_g \]

\hspace{1cm} (3.9)

\( l_g = V_f/A_c \), where \( V_f \) is the volume filtered, and \( A_c = \pi r^2 \), with \( r \) being the radius of the portion of the filter which contains the particles removed from the suspension. Also, a methanol extraction was done on the filter in order to remove the absorption due to chlorophyll pigment, leaving only the absorption due to TSS.
3.4.3 Chlorophyll a

The chlorophyll filter was removed from the freezer and the concentration of chlorophyll extracted from the filter using the procedure outlined in Standard Methods (Appendix C). The concentrations were derived both spectrophotometrically and fluorimetrically. A comparison was conducted on a few of the samples to determine if the results seemed reasonable. These results are reported along with the results of the water sample processing in Appendix D.

The uncorrected chlorophyll values are used as inputs to HydroMod, which uses the four-component model discussed in 2.1.3.2. Bukata et al. (1981) analyzed the water quality parameters of Lake Ontario using a five component model, the fifth component being nonliving organic component (NLO). They state that it is possible to use a four component model provided that the values of chlorophyll uncorrected for phaeophytin contamination, which thereby includes some detrital component.

3.4.4 CDOM

The absorption spectra of colored dissolved organic matter (CDOM) is also determined using a spectrophotometer. First, the spectrophotometer is zeroed by placing distilled water in both the reference cell and the sample cell (10 cm pathlength). Next, the water sample is filtered using a syringe filter into the sample cell. Then, the absorption spectra is recorded. The concentration of the yellow substance can be expressed as the absorption coefficient at 380 nm, \( \chi = a_y(380) (\text{m}^{-1}) \) (Spitzer and Dirks 1987). The CDOM processing results from the DIRS sampling campaign are recorded as
scalar values as seen in the Results chapter. A mean absorption spectrum was calculated from a wide range of Lake Ontario water and then ratioed against each of the water sample absorption spectra to obtain a scalar value for each sample.

3.4.5 TSS

TSS filters are placed in a heater/dryer that is located in the basement of the CIS building. The heater is set at ~150 °C and the filters are left to dry there for about 24 hours. The post-drying weight of the filters is recorded, the pre-filtered weight is subtracted, and the concentration is determined based on the amount of water that was filtered.

3.5 Bottom Target Reflectance

In addition to varying the water type, bottom type was also varied in the HydroMod runs to produce radiance values in each of the MISI bands. In order to obtain the spectra for each of the bottom types, an ASD spectrometer was used to record reflectances (ASD is the name given to the FieldSpec made by Analytical Spectral Devices, Inc.) The ASD is a portable spectroradiometer that records the reflectance spectra of the object that the "gun" is aimed at and compares it to a reference material with known reflectance properties.

The methods presented here were used as tools in the development of the approach discussed in the next chapter.
Chapter 4

Approach

In this chapter, the background information and methods presented in the previous two chapters is used in the development of an approach to gain knowledge about shallow water from a remotely-sensed image. Just as the band ratio methods improve the accuracy of depth determination over single-band methods, it often follows that using even more bands, such as in hyperspectral imagery, will further improve the results. This work consists of four major parts. First, ground truth was collected including water depths, bottom samples, and water samples. Second, the principal components analysis method was used to perform bottom type classification and water depth determination on a hyperspectral image. The third part of the research involved work with HydroMod to generate sensor-reaching radiances for different depths, bottom types, and water types that were collected in part 1. The fourth part built on parts 2 and 3; a regression was performed on the scores obtained from principal components algorithm analysis of both the image data and the model data and the errors were determined using ground truth.

4.1 The Image

The images used for this particular application were taken by the Modular Imaging Spectrometer Instrument (MISI) constructed by the Digital Imaging and Remote Sensing Group (DIRS) at RIT. MISI is a line scanning hyperspectral sensor with
63 spectral channels from 0.4 \(\mu m\) to 1.018 \(\mu m\) at approximately 0.010 \(\mu m\) intervals.

Table 4.1 shows the Band Centers for MISI.

<table>
<thead>
<tr>
<th>MISI Band Centers</th>
<th>VIS (FWHM=10 nm)</th>
<th>NIR (FWHM=8 nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>418.2962</td>
<td>754.044748</td>
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<tr>
<td>2</td>
<td>429.009263</td>
<td>762.967334</td>
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<td>771.871315</td>
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<td>448.409214</td>
<td>780.87618</td>
</tr>
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<td>467.972961</td>
<td>798.515896</td>
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<td>477.574686</td>
<td>807.440903</td>
</tr>
<tr>
<td>8</td>
<td>487.774504</td>
<td>825.065944</td>
</tr>
<tr>
<td>9</td>
<td>497.398</td>
<td>834.01772</td>
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<tr>
<td>10</td>
<td>506.996088</td>
<td>842.876596</td>
</tr>
<tr>
<td>11</td>
<td>516.928457</td>
<td>851.474834</td>
</tr>
<tr>
<td>12</td>
<td>526.484894</td>
<td>860.375241</td>
</tr>
<tr>
<td>13</td>
<td>536.063395</td>
<td>868.633836</td>
</tr>
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<td>14</td>
<td>546.026128</td>
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<td>15</td>
<td>555.924146</td>
<td>885.87757</td>
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<tr>
<td>16</td>
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<td>893.950338</td>
</tr>
<tr>
<td>17</td>
<td>574.95592</td>
<td>903.311413</td>
</tr>
<tr>
<td>18</td>
<td>584.476584</td>
<td>911.152567</td>
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<td>19</td>
<td>594.052835</td>
<td>919.083669</td>
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<td>20</td>
<td>603.982259</td>
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<td>934.554513</td>
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<td>22</td>
<td>622.507265</td>
<td>942.574798</td>
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<td>23</td>
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<td>950.564254</td>
</tr>
<tr>
<td>24</td>
<td>641.055941</td>
<td>958.448494</td>
</tr>
<tr>
<td>25</td>
<td>650.501156</td>
<td>965.709716</td>
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<tr>
<td>26</td>
<td>659.530681</td>
<td>973.463033</td>
</tr>
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<td>27</td>
<td>668.874578</td>
<td>981.01458</td>
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<td>686.558489</td>
<td>995.21763</td>
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<td>30</td>
<td>695.512074</td>
<td>1002.620013</td>
</tr>
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<td>31</td>
<td>704.448606</td>
<td>1009.525889</td>
</tr>
<tr>
<td>32</td>
<td>713.066255</td>
<td></td>
</tr>
</tbody>
</table>

Table 4.1 MISI Band Centers for Visible and NIR Bands
An advantage of MISI's hyperspectral nature is that it records a fine spectral resolution electromagnetic profile for each pixel. The wavelength-dependent characteristics in the reflectance spectra reveal important information about the optical properties of water, which can be important in water quality studies. More information about MISI and its calibration can be found in Appendix A.

The MISI images of Lake Ontario were fairly noisy. Steps were taken in order to minimize the effects of the noise. A discussion of the problems with image noise and the steps taken to correct their effects is included in Chapter 5.

4.2 Principal Components Algorithm

Philpot's principal components analysis has been performed on a synthetic data set (Philpot 1989), but there are no published examples of his approach using real data. The website, http://www.geog.ubc.ca/courses/klink/g472/class98/hamren-larsson/ (Hamren-Larsson 1998) provides information on how a principal components analysis was applied to a Landsat scene. The principal components algorithm was more accurate in predicting depths than the single band algorithm it was compared to. The PCs were linearly regressed against known depth values. However, no bottom type information was determined in this paper although bottom type variation was included as one of the factors that decreased the accuracy of the algorithm. The MISI images contain more spectral bands; and therefore, this research will test to see if more bands increase the accuracy. The algorithm was coded in the software language, Interactive Data Language (IDL) and used on images taken of the Lake Ontario shoreline by MISI in order to map
various bottom types, which were verified using ground truth collected at various points in the image. This information was useful in two ways. First, bottom type mapping near the Ontario Beach area has value to the County Health Lab, which is interested in knowing where the green algae is located. This information will help them address the issue of beach closures, which occurred 13% of the time in 1998 because of cladophora and spyrogyra washing up on the beach and decaying. A second possible use of this bottom type map be as a scene in future work with DIRSIG (DIRSIG is a first principles based synthetic image generation model developed by the DIRS program at the Center for Imaging Science (CIS)).

MISI images of the Lake Ontario shore line for summer 1999 and 2000 were available. IDL was used to code the algorithm; the software package, ENvironment for Visualizing Images, ENVI, was used to read in a variety of image formats, filter, classify, and resize images. Following is a list of steps that were taken in applying the principal components algorithm.

4.2.1 Pre-Processing

1. Mask out the land. This was accomplished in ENVI and the land was masked to a value of –1. The mask value of –1 was chosen over the typical value of 0 to account for any of the water pixels which might have a radiance value equal to 0. Masking the land increases the accuracy of the principal components analysis on the water areas in the image, because it eliminates the variability of radiance in the land portions of the image.
2. Geo-register the image. The images were manually geo-registered in Arc/Info or ENVI. This was done by matching up a Landsat image of the area containing GPS coordinates to water sampling location GPS coordinates.

3. Select deep-water areas in the image which are considered deep water. Bathymetry data were used to select areas deep enough that the bottom could not be seen. Lyzenga & Schuchman (1979) did so by averaging a set of scan lines in the along track direction in order to obtain the deep-water signal as a function of the pixel number or scan angles. The pixels selected as deep water were averaged to form a single deep-water observation.

4. Address the noise problems, as discussed in Chapter 4.

4.2.2 Deep Water Correction

1. Linearization of data. The simple radiative transfer equation for optically shallow waters is linearized. The parameter $X$ is found, such that

$$X = \ln(L_d - L_a) = \ln(L_a) - g\tau$$  \hspace{1cm} (4.1)

2. Plot the data in linearized feature space to visually determine if there are nonlinearities and if there are clusters which indicate different bottom types.

4.2.3 The Algorithm - Depth

1. Form a matrix of all $X$ calculations and perform an eigenvector analysis on the $X$ matrix. Use a plot of the eigenvalues in order to determine how many principal components to retain. The SCREE plot method, a graphical technique that retains the
eigenvalues that are to the left of the break in the plot, is used. The last eigenvalues tend to be small and in a straight line; the eigenvalues retained are before the plot levels out. (Jackson 1991) The first principal component is assumed to be the optimal coefficient vector, \( \mathbf{a}_{\parallel} \). Knowing \( \mathbf{a}_{\parallel} \) will allow for determination of \( Y_{\parallel} \): 

\[
Y_{\parallel} = \mathbf{a}_{\parallel} \mathbf{X} = \mathbf{a}_{\parallel} \ln(\mathbf{L}_{\parallel}) - (\mathbf{a}_{\parallel} \mathbf{g}) \mathbf{z}
\]  

(4.2)

For the remainder of the discussion, this depth dependent variable will be referred to as \( Y \).

4.2.4 The Algorithm - Bottom Type

In addition to depth information, the variation in bottom types will be mapped.

1. For each bottom type, determine \( \mathbf{a}_{\perp} \), which is the eigenvector perpendicular to \( \mathbf{a}_{\parallel} \), and can be used to characterize the depth independent variable \( Y_{\perp} \):

\[
Y_{\perp} = \mathbf{a}_{\perp} \mathbf{X} = \mathbf{a}_{\perp} \ln(\mathbf{L}_{\perp})
\]  

(4.3)

Notice this variable is entirely independent of depth, since \( \mathbf{a}_{\perp} \) is perpendicular to \( \mathbf{a}_{\parallel} \) \( \mathbf{a}_{\perp} \mathbf{g} = 0 \), and the depth-related term drops out of the equation.

2. Use the depth-independent variable for the bottom type, \( Y_{\perp} \), to perform a classification on the image. For this task, the k-means unsupervised classification capability of ENVI will be used. The bottom type map is actually a one band image and
therefore the unsupervised classification is really a gray-level slice which classifies the
data in the $Y_1$ image based on brightness.

The next step is to determine how well the algorithm performed and determine some
quantitative information about depth and bottom type. It is preferable to do this without
performing an extensive ground truthing effort of diving and sampling the bottom of the
lake, so a principal components regression is performed first on the HydroMod radiance
values in order to determine regression coefficients which are then applied to the
principal component algorithm-processed images (Philpot 1989). This assessment takes
advantage of the flexibility of the model, HydroMod. The concentrations of TSS,
Chlorophyll $a$, and CDOM gathered from DIRS data collections were used as inputs to
HydroMod. Then, both bottom type and depth were varied in order to generate sensor-
reaching radiance values for use in the PCR.

4.3 Inputs to HydroMod

In order to use PCR, the conditions under which the images were taken need to be
modeled as closely as possible; therefore, the characteristics of the intervening water
column must be known. This requires an extensive water sampling campaign and water
processing to determine various concentrations that will serve as inputs to HydroMod.
This research takes full advantage of the features of HydroMod which takes into account
the atmosphere, water reflectance, water quality, and bottom reflectance in order to
provide the sensor reaching radiance. The details of the program HydroMod can be
found in Fairbanks (1999). The water sampling and filtering processes were presented in
Chapter 3. The results of this processing and bottom reflectance measurements were used to build the forward model.

4.4 The Forward Model

The inputs to HydroMod will simulate as closely as possible the conditions under which the images were recorded. The components of this forward model built to calibrate the principal components regression (Section 3.3) are shown in Figure 4.1.

![Figure 4.1 Components of the Forward Model](image)

The radiosonde data from the image collection day will be used to calculate the effects of the atmosphere. Radiosonde is a term that refers to the instrument package that collects and transmits meteorological data, and is carried into the atmosphere by a weather balloon. Although HydroMod includes the capability to add clouds to the scene, this option will not be used; because the images were taken on clear days. The water quality parameters are derived from the filtering and subsequent processing of the water samples. The default absorption cross-sections and scattering cross sections (Figs. 2.5-2.8, respectively) are based on Lake Ontario (Bukata 1995) and updated cross-sections determined from water samples collected on May 20, 1999.
A different bottom boundary will be created using the bottom type reflectances discussed in Section 3.5. From the HydroMod User's Manual, it seems that only a wavelength independent reflectance is allowed if the "User Supplied Constant Reflectance" option is selected. This is not an acceptable option because bottom reflectances vary with wavelength; therefore, HydroMod will need to be modified in order to add the bottom types characteristic of the area captured in the image. The reflectance spectra needed – Lake Ontario sand, cladophora and/or spyrogyra, and additional spectra – will have to be collected.

HydroMod runs at various depths with various bottom and water types were made. The resulting sensor-reaching radiance values will be put into a matrix for use in the PCR discussed in the next section. Table 3.3 shows the various depths, bottom types, and water types that will be used in a factorial method.

<table>
<thead>
<tr>
<th>Bottom Types</th>
<th>Depth (m)</th>
<th>Water Type</th>
<th>Sample</th>
<th>Chl (mg/m^2)</th>
<th>TSS (mg/L)</th>
<th>CDOM (scalar)</th>
</tr>
</thead>
<tbody>
<tr>
<td>#     Name</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1     Ontario sand</td>
<td>0.5</td>
<td></td>
<td>I1</td>
<td>0.934</td>
<td>1.000</td>
<td>0.451</td>
</tr>
<tr>
<td>2     Hydromod Green Algae</td>
<td>1.0</td>
<td></td>
<td>A5</td>
<td>1.145</td>
<td>1.000</td>
<td>0.485</td>
</tr>
<tr>
<td>3     Gray Rock1_wet</td>
<td>3.0</td>
<td></td>
<td>A3</td>
<td>1.671</td>
<td>1.333</td>
<td>0.481</td>
</tr>
<tr>
<td>4     Gray Rock2_wet</td>
<td>5.0</td>
<td></td>
<td>A6</td>
<td>1.698</td>
<td>0.750</td>
<td>0.454</td>
</tr>
<tr>
<td>5     Red Rock with algae2</td>
<td>7.0</td>
<td></td>
<td>A2</td>
<td>1.868</td>
<td>1.000</td>
<td>0.467</td>
</tr>
<tr>
<td>6     RedRock1_wet</td>
<td>10.0</td>
<td></td>
<td>I4</td>
<td>3.463</td>
<td>2.400</td>
<td>0.438</td>
</tr>
<tr>
<td>7     Light gray rock1_wet</td>
<td>30.0</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8     Yellow rock1_wet</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 4.2 Inputs to HydroMod

The inputs from Table 4.2 are used to build the forward model, which is then used to calibrate the principal components regression.
4.5 Applying Principal Components Regression to this Research

Principal components regression is a statistical tool that combines principal components analysis with regression. For multiple observations, the independent variable of the regression, \( X \) forms the matrix defined below for \( L_{\text{obs}} \) = the dependent variable:

\[
X = \begin{bmatrix}
1 & Lobs_1(\lambda_1) & \ldots & Lobs_{L_{\text{obs}}}(\lambda_1) \\
1 & Lobs_1(\lambda_2) & \ldots & Lobs_{L_{\text{obs}}}(\lambda_2) \\
\vdots & \vdots & \ddots & \vdots \\
1 & Lobs_1(\lambda_p) & \ldots & Lobs_{L_{\text{obs}}}(\lambda_p)
\end{bmatrix}
\]

(4.4)

where \( p \) = number of bands and \( n \) = number of observations.

Then, the linear regression equation to determine the matrix of regression coefficients, \( b \), is

\[
b = X^{-1}Y
\]

(4.5)

which is actually calculated as

\[
b = \left(X^T X\right)^{-1} X^T Y
\]

(4.6)

For the PCR, the regression described in the preceding section will be performed not on the \( X \) matrix itself, but on the scores matrix, which is determined by multiplying the \( X \) matrix times its principal components. The following equation shows in matrix
form how one principal component score (PC) is obtained by multiplying an eigenvector, a, by the data, L(λ).

\[
\begin{bmatrix}
PC_1 \\
\vdots \\
PC_n
\end{bmatrix} =
\begin{bmatrix}
a_0 \\
a_1 L_t(\lambda_t) L \\
\vdots \\
a_p L_t(\lambda_p)
\end{bmatrix}
\]

(4.7)

Again, p = number of bands and n = number of observations.

Instead of performing a regression directly on the spectral responses, this method regresses the concentrations on the PCA scores. The PCA scores are the result of transforming the data using the principal components, so in other words, an observation is transformed using the first principal component (eigenvector), resulting in the score. According to Galactic Industries Corp. (2000), using the eigenvectors to calculate the regression instead of the spectral responses themselves “produces a robust model for predicting concentrations of the desired constituents in very complex samples”. This is because the eigenvectors of the principal components analysis represent the spectral variations common to all of the calibration data.

Eq. 4.8 is the principal component regression equation that will be used in this research. The assumption is made that varying depth, bottom type, and water type account for the greatest variation in the data. Therefore, only the first three principal components (PCs) will be retained for the PCR against the dependent variables, depth.
(d), bottom type (bt), and water type (wt) from which the regression coefficients, b, will be calculated.

\[
\begin{bmatrix}
d_1 & bt_1 & wt_1 \\
\vdots & \vdots & \vdots \\
d_n & bt_n & wt_n \\
\end{bmatrix} = \begin{bmatrix} 1 & PC1 & \ldots & PC3_1 \\
\vdots & \vdots & \vdots & \vdots \\
1 & PC1_p & \ldots & PC3(\lambda_p) \end{bmatrix} \begin{bmatrix} b_0 \\
\vdots \\
b_2 \end{bmatrix}
\]

\[
Y = X b
\]

(4.8)

4.5.1 PCR Applied -- HydroMod

The HydroMod runs will be used to calibrate the PCR because both the inputs (depths, water components, bottom types) and the outputs (radiances) are known. In an effort to model the image as closely as possible, the radiosonde file for the day (September 3, 1999) was used to build the sky files in MODTRAN as part of HydroMod. Also, the water components used will be the constituents actually found in the water samples collected in the Ginna area.

The steps for implementing PCR on this data are as follows:

1. Perform deep water subtraction on the X matrix by subtracting the radiance values calculated for a depth of 30m, and take the natural log of the data (Philpot’s 1989 algorithm).
2. Calculate the covariance of the X matrix from Step 1.
3. Determine the eigenvectors. These are the coefficients for the linear combination that maximize the variance in the data. Only the depth, bottom type, and water
type were varied in the HydroMod runs. Therefore, only the first three
eigenvectors will be retained (A).
4. Determine scores for the retained eigenvectors. \( \mathbf{PC} = \mathbf{XA} \)
5. Perform the regression. Use the pseudoinverse to calculate the regression
coefficients, \( \mathbf{b} \).

\[
\mathbf{b}_{\text{Hydro}} = (\mathbf{PC}^T \mathbf{PC})^{-1} \mathbf{PC}^T \mathbf{Y}
\]

The \( \mathbf{Y} \) matrix here represents the inputs to HydroMod.
6. Calculate \( \mathbf{Y}_{\text{est}} \). \( \mathbf{Y}_{\text{est}} = \mathbf{PC}_{\text{Hydro}} \)
7. Compare the results. The depth estimate, for example, is the first column of the
\( \mathbf{Y}_{\text{est}} \) matrix. Compare this value to the actual depth input into HydroMod using
root mean squared (RMS) error,

\[
\frac{1}{N} \sum_{i=1}^{n} (d_i - \hat{d}_i)^2 = \text{MSE} \quad \text{RMS} = \sqrt{\text{MSE}}
\]

4.5.2 PCR Applied - The Image

The next steps involve implementing Philpot's algorithm and PCR on the image.

1. Select an area of the image which can be assumed to be deep water. Average
some of these deepwater pixels.
2. Subtract the deepwater pixel from the rest of the image.
3. Take the natural log of this deepwater subtracted image (Philpot's \( \mathbf{X} \) matrix).
4. Calculate the covariance of the data. (\( \mathbf{X} \))
5. Determine the eigenvectors (\( A \)). These are the coefficients, or weights. Most
likely only the first three eigenvectors will be retained based on looking at a plot
of the eigenvalues.
6. Calculate scores. \( \mathbf{PC}_{\text{image}} = \mathbf{XA} \)
7. Using the \( \mathbf{b} \)s calculated from the above HydroMod Step 5, estimates for the
dependent variables, depth, bottom type, and water type are found.
\( \mathbf{Y}_{\text{est}} = \mathbf{PC}_{\text{image}} \mathbf{b}_{\text{Hydro}} \)
8. Compare the results with ground truth. For example, for depth, compare depth
estimates with actual bathymetry.
Chapter 5
Results

5.1 Data Collection

Often, data collection for this research was at the mercy of the weather, functioning instruments, and boat availability. Although sometimes data collection was frustrating, it was also very rewarding because the location for data collection was Lake Ontario, usually on a boat on a beautiful, sunny day. The data needed for this research consisted of water samples, bottom type samples, and the images themselves.

5.1.1 Water Sampling

Water was collected under Landsat and MISI overpasses in order to characterize the water at the time the images were taken. The sample bottles were rinsed out twice with lake water prior to filling them up with water at each sampling location. The water sampling days and locations for 1999 and 2000 are shown in Table 5.1.
Table 5.1 Water Sampling Dates and Locations – 1999 and 2000.

The water samples were filtered and processed as explained in section 3.4. The results of the processing of the 1999 samples will be located on the following website, http://www.cis.rit.edu/research/dir.shtml. Information on the September 3 1999 processing is located in Appendix D. The water parameters used for the HydroMod portion of this research are from the samples taken at Ginna on 3 September. Table 5.2 shows the sample number and the results of processing.

<table>
<thead>
<tr>
<th>Sample</th>
<th>CHL-a (mg/m^3)</th>
<th>TSS (mg/L)</th>
<th>CDOM (scalar)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A2</td>
<td>1.868</td>
<td>1.000</td>
<td>0.467</td>
</tr>
<tr>
<td>A3</td>
<td>1.671</td>
<td>1.333</td>
<td>0.481</td>
</tr>
<tr>
<td>A5</td>
<td>1.145</td>
<td>1.333</td>
<td>0.485</td>
</tr>
<tr>
<td>A6</td>
<td>1.698</td>
<td>0.750</td>
<td>0.454</td>
</tr>
<tr>
<td>I1</td>
<td>0.934</td>
<td>1.000</td>
<td>0.451</td>
</tr>
<tr>
<td>I4</td>
<td>3.463</td>
<td>2.400</td>
<td>0.438</td>
</tr>
</tbody>
</table>

Table 5.2 Sampling Results for Ginna, September 3, 1999
Of note are the high chlorophyll and TSS values for the last sample, I4. These relatively high concentrations from sample I4 will manifest themselves in both the qualitative results from the algorithm processing and the radiance outputs from HydroMod.

These data were input into HydroMod in order to simulate as closely as possible the conditions under which the MISI images were taken. In order to be more accurate in simulating these conditions, bottom reflectances were also needed.

5.1.2 Bottom Sampling

The ASD was used to take reflectance spectra of various materials assumed to form the bottom boundary at the Ginna site near the power plant, based on visits to the area. This data collection requires a clear day in order to have consistent lighting conditions. To calculate the reflectance spectra, a Spectralon white reference is used to account for the lighting conditions.

The bottom at Ginna consists predominantly of rock and algae-covered rock. Therefore, a variety of rock spectra, and even spectra of algae-covered rock were collected. There is also some sand in the area, and so, this spectrum was included in the model. The following figures include images and spectra of the bottom types that were input into HydroMod to build the forward model.

Figure 5.1 is a graph of sand spectra: one is built into HydroMod, and the other was the spectrum of Ontario sand measured by the ASD. The bottom reflectance spectrum that is used for sand in these HydroMod runs is Ontario sand. The other sand
reflectance spectrum is inherent in the HydroMod program; however, it is for bright coral sand, and is not indicative of the sand found on the bottom of Lake Ontario.

Figure 5.1 Hydromod Sand vs Ontario Sand – Reflectance Spectra

Figure 5.2 Green Algae Bottom Type in HydroMod
Figure 5.2 shows the green algae bottom that will form another bottom type used in the HydroMod runs. Actual reflectance spectra were collected of algae dredged from the bottom of the Lake near Charlotte Pier. The spectra had a similar shape as that of Figure 5.2; however, the magnitude was lower, due to the fact that the algae was dying. It was dark green and had a decaying odor. Therefore, the decision was made to use the HydroMod green algae spectrum because the bottom type that needs to be modeled is of live, benthic algae.

The following figures are images and spectra of various rocks and algae-covered rocks measured at Ginna on July 20, 2000. The various spectra will be inputs to HydroMod, representing different bottom types.
Figure 5.5  Gray Rock 2 (Groc2)

Figure 5.6  Groc2_wet input to Hydromod

Figure 5.7  Red rock (redrock_wet)

Figure 5.8  Redrock_wet input to Hydromod

Figure 5.9  Algae on Red Rock (Rro_alg2)

Figure 5.10  Rro_alg2 input to Hydromod
These bottom types are all characteristic of the Ginna area. The Ontario Beach area is characterized by the green algae spectrum and the Ontario sand spectrum. However, a visit to the coastal waters near Ontario Beach revealed that the algae is found growing on rock that is dark in color. The reflectance spectrum needs to be collected for the rock
found out near Ontario Beach in order to model accurately the parameters that form the MISI images of this area.

Bottom sampling was also conducted as part of ground truth collection. In order to sample the bottom, a Fieldmaster bottom dredger (Fig 5.15) was used. It is set open and dropped to the bottom. When it hits the bottom, it closes, scooping up whatever is there. At Ginna, it frequently hit rock, and therefore, nothing was pulled up.

![Bottom Dredger](image)

Figure 5.15 Bottom Dredger

This verifies, though, that the bottom consists of rock. The results of the ground truth are discussed in Section 5.5.5 for Ontario Beach.

5.2 MISI Images

The MISI images of the Charlotte Pier (Ontario Beach) and the Ginna Power plant were challenging to work with. Steps were taken to correct the significant noise problems observed in the MISI data. First, a low pass filter was convolved with the image, but upon analysis of each of the 63 bands, a significant amount of vertical banding and
horizontal streaking remained. Also, there were some bands that were unintelligible even after they were convolved with a low-pass filter (Fig. 4.16 and 4.17)

Figures 5.16 and 5.17 Band 12 and Band 20 Noise Problems in C9 (Ginna)

In addition to convolving the image with a low-pass filter, some of the worst bands were discarded prior to implementation of Philpot’s algorithm. On the September 3, 1999 Ginna image (C9, Flight Line GFL2) that was taken perpendicular to shore, an area of the image was selected that began near the shore and went out perpendicular from shore. After some of the worst bands were discarded, 51 remained. The image used here to discuss the noise problems was 116 by 258 by 51 (Ginna_four) and is shown in Figure 4.18.
After initial noise processing, the principal components algorithm (Philpot 1989) was implemented on the image in an effort to determine water depth and bottom type information. $Y_\parallel$ refers to the image obtained by multiplying the first eigenvector times the $X$ matrix (linearized variable), and is assumed to provide information about depth; $Y_\perp$ refers to that image obtained by multiplying the second eigenvector times the $X$ matrix, and is assumed to provide information about bottom type. The principal components algorithm (Philpot 1989) was run on this image (Fig. 5.18) and then both the $Y_\parallel$ image and the $Y_\perp$ image were read into ENVI. A simple unsupervised $k$-means classification was performed to determine which image areas are similar. The $k$-means classification is performed on a single-band image, $Y_\parallel$ or $Y_\perp$, and therefore is simply a gray-level map showing areas of similar brightness rather than a classification, which is typically done on
multi- or hyperspectral images. Figures 5.19-22 show the $Y_{\parallel}$ images and their respective gray-level maps.

Figure 5.19 $Y_{\parallel}$ on Ginna_four(Fig. 5.18)  
Figure 5.20 $Y_{\parallel}$ on Ginna_four classified

Figure 5.21 $Y_{\perp}$ on Ginna_four  
Figure 5.22 $Y_{\perp}$ on Ginna_four classified
The greatest variation in the original image, highlighted by the algorithm and displayed in these images, appears fairly structured. It looked very much like the vertical banding seen in the NIR bands, two of which are shown in Figures 5.23 and 5.24.

From these images, one can see that the vertical, wavy banding and the pattern that shows up in the algorithm-processed images are similar. The NIR bands don’t penetrate very deep into the water, and therefore carry little information, with most of the signal due to noise.

Using ENVI, the image was spectrally resized again, deleting the NIR bands from the new image, ‘Ginna_seven’ (Fig. 5.25). The figures below show these results and from them one can see that the banding structure no longer is a significant part of the transformed images.
Additional steps were taken to improve the images prior to processing. First, median filtering was performed on the image, using a 5 x 5 median filter in ENVI. This helped alleviate some of the salt and pepper noise. Next, the image was convolved with a 5 x 5 low-pass filter to further blur some of the remaining noise effects. In an effort to increase the signal to noise of the image, the REBIN function in IDL was used to shrink the image spatially by averaging neighboring pixels, while still maintaining the spectral resolution,
although the spectral structure is degraded some due to the mixing of the adjacent pixels. Then, the same function restores the spatial dimensions of the image, using the default bilinear sampling on the expansion. After all of this processing, there were still bands that needed to be discarded, mostly in the NIR. A majority of the results discussed in this section were obtained by performing the principal components algorithm (Philpot 1989) on the September 3, 1999 Ginna image, C9 (Fig. 5.29). After pre-processing the image to reduce noise, only 24 bands were retained, shown in Table 5.3.

<table>
<thead>
<tr>
<th>C9 MISI Band</th>
<th>From (nm)</th>
<th>To (nm)</th>
</tr>
</thead>
<tbody>
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<td>423.2962</td>
</tr>
<tr>
<td>2</td>
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<td>32</td>
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Table 5.3 Ginna (C9) MISI Bands retained for algorithm
5.3 Image Selection

Philpot’s algorithm (1989) was implemented on an image called C9 after noise processing. The image is shown in Figure 5.29.

Figure 5.29 C9 – R,G,B, Image of Ginna

Philpot’s algorithm (1989) depends on a deep-water subtraction. Many of the images taken during flight lines parallel to shore do not contain deep-water pixels. A benefit of using this image is that deepwater pixels taken at the same angle as the image can be selected. A second benefit of using this image is that the Ginna area has a lot of variation in it. Figure 5.30, a smaller piece of C9, shows the variation in bottom type near the shore, which the algorithm will extract.
Figure 5.30 Smaller portion of Image C9 showing coastal bottom type variation

An aspect of this image, which will be discussed later in this Chapter, is the bright blue area of water at the left side of Figure 4.30. This image characteristic provided a challenge in implementing Philpot's (1989) algorithm on Case 3 data, where the water type varies, and in this image, the water type variation is apparent from the image. The very bright blue corner, A, is most likely due to a phytoplankton bloom that was occurring at the time this image was taken and was noted during water sampling on September 3 (corresponding to sample 14 discussed in Table 5.2). The slightly darker water, B, is most likely due to a combination of different water type and lighting conditions and C is an area where the water type appears darker than both A and B. The
image was taken at 11:19 EST, which means that the sun was more towards the left side of the image (east), resulting in a variation in lighting conditions.

Although most of the results were calculated from the September 3, 1999 image of Ginna, one of the MISO images taken on July 5, 2000 near the Charlotte Pier, C2 (Flight Line RFL1), was also processed (Fig. 5.31). These images were taken parallel to the shore, and therefore were not ideal, because there is not much deep water. The deep-water pixels are selected from an area of the image that was not at the same angle relative to nadir as that area being processed by the algorithm. However, one of the goals of this research is to see how well the algorithm performs on images taken of this portion of Lake Ontario, since it experiences many problems due to algae washing up on the shore. The images from this day have some missing lines, so a smaller area of image C2 (Fig. 5.31) was selected that did not have missing lines and contained land references easily recognizable from the water for ground truth purposes.
5.4 Qualitative Results

After applying Philpot's (1989) algorithm to various small pieces of the C9 image, the next step was to look at bigger areas of the image. In order to do this, the algorithm must be able to perform the eigenvector analysis on just the water pixels, because applying the algorithm to the entire image, including the land, decreases the likelihood that the variability of interest is in the first two eigenvalues, if any of them. The image, C9, was resized both spatially and spectrally in ENVI to produce an image that contains the shallow water and eliminates the noisy bands, resulting in a 24-band image, the bands shown earlier in Table 5.3. The depth and bottom type maps are a result of k-means
unsupervised classifications, which essentially are just the gray-level maps discussed earlier, on the $Y_{H}$ and $Y_{L}$ images, for which areas that are similar in brightness are grouped in the same class.

5.4.1 Using the Entire Width for Deep-Water

Usually, deep-water pixels are selected such that they cover the same columns as the image. However, in C9, there was an obvious difference in water type further out in the image, which might affect the results. Figure 5.32 is the image, called Ginna for discussion purposes, and the corresponding deep water taken over the entire width of the original image, C9 (Fig 5.29).

![Figure 5.32 Image Ginna and the deepwater taken over the entire width of the image](image)
Of note is how light the pixels are on the left side of the deepwater image. The deepwater pixels were averaged and the resulting vector was subtracted from each of the pixels in the Ginna image. The next step in this deep-water correction technique is to calculate the natural log of the resulting matrix. The final result of this deep-water correction is the linearized variable, X. Plotting the X values for the 640 nm vs 545 nm band should show that there is a somewhat linear relationship between the two linearized variables, $X_{640}$ and $X_{545}$, provided the water type is constant. Figure 5.34 is a scatter plot of these two bands in linearized space for the colored section of the image in Figure 5.33.

Next, the principal components analysis was performed on the linearized data. The first principal component points in the direction of maximum variance in the data set, showing that a linear combination of the variables $X_{640}$ and $X_{545}$ using the optimal coefficients (first eigenvector) indicates the information that is correlated between the two bands.

Figure 5.33 Y for Ginna image processed using the entire width of C9 for deep water (colored portion corresponds to 5.34)  

Figure 5.34 Scatter plot of $X_{640}$ (Band 24) vs. $X_{545}$ (Band 15) using the entire width of C9
This plot is not linear, which is an indication that an assumption has been violated. The scatter plot should be linear if the water type is constant, which is not true of this example. The deepwater term, \( L_m \), used in the principal components algorithm (1989) is also presumed constant, but when this is not a valid assumption, the usual linearization is no longer suitable, and attempting to use it results in the nonlinearities seen in the scatter plot (Fig. 5.34).

Further analysis of the scatter plot and its corresponding regions in the image reveal other inconsistencies. The red and green regions of the image (Fig 5.33), which, based on their position in the scatter plot, should correspond to the shallow areas of the image, seem reasonable, but the next region (yellow) based on the scatter plot should be getting shallower because the yellow points start to spread towards the top of the plot, also shows up near the left side of the image. Intuition and bathymetry confirm that this trend of getting deeper as one moves away from shore and then shallower again further out is due to error in the assumptions made. The blue area in the image corresponds to pixels in the scatter plot that are in a very shallow area due to their location near the top of the plot. However, considering the location of the blue region in the image, this does not make sense, and results from a combination of the different water types, i.e. water with different optical properties, in the image being processed by the principal components algorithm and from using the entire width of the image, which contains different water types, for the deep water. The deep-water correction of the algorithm
subtracts off the averaged deep-water pixels and therefore does not take into account the fact that the image being processed contains different deep and shallow water types. The next figures show the depth map and bottom type map resulting from using the entire width for deep water.

Figure 5.35 $Y_{\parallel}$ - deepwater of entire image

Figure 5.36 $Y_{\perp}$ - deepwater of entire image

These maps do not seem reasonable, as might be expected based on analysis of the scatter plot in Fig 5.34. In Figure 5.35, the depth map, the water gets deep and then shallow again as one moves away from shore. There is deeper water (yellow) near the shore. From water truth observations, the trends in the depth map are not true. Figure 5.36 is not picking up on the bottom type variation that is visible from the image itself. It is also very similar to Figure 5.35 in appearance, which was not expected because it is a bottom type map.

Next, the technique was repeated, choosing a different area for deep-water pixels.
5.4.2 Using Darker Deep-Water

The algorithm was performed on the same shallow water image, Ginna, but the deep-water pixels were selected from the right side of the image C9 as shown in Fig 5.37.

Figure 5.37 Ginna image and deepwater from the right side of the image, C9

The deepwater image in Figure 5.37 is noticeably darker than that shown in 5.32, which used the entire width of the image. The left side of the deepwater image is still brighter than the right side due to stretching in ENVI. Once again, the average of the deep-water pixels was calculated and the algorithm applied, as above, resulting in improved depth and bottom type maps. Figure 5.39 is the scatter plot of the linearized variables, $X_{540}$ vs $X_{545}$, and it is closer to the expected linear plot that should result when the water type is constant.
Figure 5.38 $Y_{nd}$ for Ginna processed with deep water from right (colored portion corresponds to Fig. 5.39)

Figure 5.39 Scatter plot of $X_{640}$ (Band 24) vs. $X_{545}$ (Band 15) using the right side of C9 for deepwater

The colors of the scatter plot represent the data that correspond to the regions of the image in Figure 5.38. The linearization performed better at smaller depths, but where the scatter plot spreads out at greater depths, the results depart from intuition. The dark green class at the left side of the image corresponds to the portion of the scatter plot pointed to by the arrow. If our assumptions are correct, this dark green area is more shallow than the sea-green region of the image. However, the dark green region is located at the very left of the image, where the water should be the deepest. This inconsistency is probably a result of the dark deepwater being subtracted from an area of different water type, and the greatest variation is no longer related to depth, but is now associated with a change in water type. The shallow areas of the image correctly correspond to the right side of the scatter plot, although caution is required in
interpretation because this may be an area where water type varies with depth. The uncertainty of the depth estimate increases greatly with depth, as can be seen in Figure 5.39, indicated by the spreading out of the graph as the depth increases.

Figure 5.40 is a plot of the eigenvalues for this image. The first eigenvalue, the amount of variability assumed to be due to depth, accounts for 41% of the variability. The second eigenvalue, variability assumed to be related to bottom type, accounts for 21% of the variability in the data.

![Eigenvalues](image)

**Figure 5.40** Eigenvalues from PCA on Ginna image processed using deep water from the right side of C9

The first three bands carry most of the variability in the data. In this example, the variability accounted for in the first eigenvector does not totally correspond to depth variation but also includes some variation due to change in water type. Similarly, the second eigenvector is mixed because as soon as the first eigenvalue is mixed, the remaining eigenvalues must also be mixed due to their perpendicular nature.

The depth map and bottom type map determined using the deep-water from the right side of the C9 image seem more reasonable than the previous example (Fig. 5.32).
Figure 5.41 Y using deep water from right (~Depth)

Figure 5.42 Yperp using deep water from right (~Bottom Type)

Figure 5.41 is more intuitive than the depth image calculated when the entire width of the image was used for deep-water. The first four classes (cyan, yellow, blue, and then green in order of decreasing brightness) show that the water gets consistently deeper as one moves out from the shore, as one would expect. But, the results show again that the water gets deeper and then shallow, so that the area one would expect to be deepest (the bottom left corner of Fig 5.41) is actually shown to have a similar score, i.e. is as shallow as, the water right off the coast (cyan class). The algorithm is equating the brightness in the lower left corner of the Ginna image presumably caused by different water type to shallow water. Figure 5.42 is a great improvement over the bottom map from the results processed using the entire width of the image for deep-water (Fig. 5.36). Fig. 5.43 points out where the bottom map seems to be discerning bottom-type variations that are visible in the image.
Figure 5.43 $Y_{\perp}$ (−Bottom type) is picking up on variations in Ginna image

The cyan class on the left side of the $Y_{\perp}$ image is still problematic. This is due to the deep water not being consistent with the water qualities in the rest of the image. It can be inferred that the bottom type mapping, like depth mapping, performs better at smaller depths, which is most likely because there is less effect due to water-type variation in shallow water.

The qualitative effects of variable water type in the deepwater pixels are significant. Further processing was done on smaller portions of the image where there appeared to be constant water type.

**5.4.3 Consistent Deep Water**

Figure 5.44 shows the image selected from the right side of the image (Ginna_right) and its respective deep-water image that was used to perform the algorithm.
Figure 5.44 Image and Deep_water from the Right Side of Ginna

Figure 5.45 Ginna_right with colors corresponding to 4.45

Figure 5.46 Scatter plot of $X_{545}$ (Band 15) vs. $X_{640}$ (Band 24) for Ginna_right
The results from processing with these images are very encouraging. Fig. 5.46 exhibits much more linear behavior, indicating that the information in these bands is more closely correlated in the linearized space and that there are fewer unmodeled factors.

Statistically, the information was pretty highly correlated before, but this does not always mean that the correlation provides the information desired. The trend in Fig. 5.47 is very intuitive, the water gets deeper as one moves away from the shore. Below are the depth and bottom type maps.

Figure 5.47 $Y_{nl}$ (depth) – k-means classification of Ginna_right using 3 classes and 4 classes, respectively

These results are very reasonable; the water gets consistently deeper as one moves out from the shore. Looking at 2 m resolution bathymetry from this area confirms this trend.
Figure 5.48 $Y_\perp$ (bottom type) using 3 and 4 classes, respectively and comparison to actual image. Arrows indicate where bottom type variation seen in the image shows up in the bottom type maps.

This bottom map is reasonable, however it appears that using three different gray-level brightnesses is sufficient for distinguishing the different bottom types. The bottom type map highlights some of the major variations that can be seen in the image, and there are problems with the varying water types seem to be eliminated.

The algorithm performs better when the deep water is the same, or nearly the same, water type as the image being processed as in this example. The results do not
contain the non-linearities evident in the example discussed in Section 5.4.1, which used the entire width of the image as the deep water. The depth map and bottom type map agree with intuition and analysis of the image.

In summary, to obtain good results, one must select an area in which the water type is constant over the image and the deep water, there are depth variations, and bottom variations. This is a limitation of the principal components analysis approach in that it depends on the image selection.

5.4.4 More Results

Attempts were made to select other areas in the image where the water type was thought to be constant, although the efforts were not as successful as that in Sec. 5.4.3.
An interesting feature of the depth maps of both images is a narrow region (red) that indicates some sort of trench, or area of deeper water. The “trench” corresponds to the line where the water becomes deep very quickly as indicated by the drop-off in the ability to see the bottom variation in the image. The “trench” shows up in both depth maps, which were produced using eigenvectors from different principal component analyses. The bottom maps again are highlighting variations in bottom type that can be seen in the images themselves.

The algorithm performs better on smaller sections of the image because there are typically not as many variations, such as water type, over a small area. The variations that will most likely be present in an image that covers a greater spatial region are not limited to varying water type, but might include atmospheric conditions, illumination, and sea state.

5.4.5 Ontario Beach Results

In order to determine the feasibility of mapping the distribution of benthic algae in the Ontario Beach area to benefit the County Health Lab, a preliminary analysis was done on a MISI image taken of the area July 5, 2000. The image selected for this analysis was C2 (Fig. 5.51). This image was selected because it was taken at a higher altitude than some of the other images; this is significant because more water is included in the image, which is important in deep-water selection. Also, it was one of the better-quality images in terms of noise, missing lines, and sun glint through the middle of the image.
image. The flight line for this image was parallel to shore, and therefore, it is almost certain that the deepwater pixels are not at the same angle relative to nadir as the part of the image being processed. This effect was not corrected for in this analysis.

Although this was one of the better images from the July 5, 2000 MISI collect, the sun glint can be seen down the middle of the image C2, and is present on the right side of Ont_one. Below (Fig. 5.52 - 5.55) are the results of applying the algorithm to this image. The deepwater was selected from the extreme right of the image (C2) because there is not
a significant amount of water that appears to be deep enough to not be influenced by the bottom type.

The depths and bottom types are correlated in this image. Analysis of Figs. 5.52 and 5.53 indicates that there are ridges on the lake floor and the depth alternates between shallow and deep with these ridges. The bright area (green in Fig 5.53) on the right of 5.52 is due
to the sun glint effect and is not related to depth. The shallow areas (green) correspond to the light areas in Fig. 5.54, which are of sand bottom type, based on ground truth. The deeper areas (red) correspond to the dark areas in Fig. 5.54, which indicate rock bottom type. The change in depth has been verified by ground truth.

These preliminary results are very promising for the application of this algorithm to MISI images in order to determine the location of benthic algae. The algae attach themselves to hard surfaces, i.e. rock. At one sampling location, a small amount of algae was grabbed from the rock bottom with the dredger.

The depth changes and bottom type changes in Figs. 5.53 and 5.55 were verified by ground truth. Fig. 5.56 shows the sampling locations and data for this image, which was collected on July 30, 2000.

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<td>2</td>
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<tr>
<td>2</td>
<td>Sand</td>
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<tr>
<td>3</td>
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<tr>
<td>4</td>
<td>Sand</td>
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Figure 5.56 Ground Truth Results for Ont_one
5.5 Building the Forward Model

The HydroMod model was run for September 3, 1999 atmosphere and water conditions. The water types that were input were based on the water sampling campaign and subsequent processing of the samples. The results for sampling are in Appendix D. The output for each of the HydroMod runs was water-leaving radiance. For the purposes of comparison to the algorithm output, the sensor-reaching radiance was needed. To get the radiance to the sensor, it was necessary to multiply by the transmission and then add upwelled radiance for the September 3, 1999 atmosphere. Figure 5.57 shows the upwelled radiance and transmission information for September 3, 1999 conditions sampled at MISI wavelengths. These values were obtained using MODTRAN.

Figure 5.57 Transmission and Upwelled Radiance for September 3, 1999
One run was performed, with the bottom reflectance set to zero at every band in order to determine the radiance due to the water column itself. Fig. 5.58 is a plot for the various water types at various depths over the zero reflectance bottom.

![Zero Reflectance Bottom](image)

**Figure 5.58 Plot of Sensor-Reaching Radiances for a Zero-Reflectance Bottom**

The spectra with the greatest radiance in the plot are from the water sample I4, which contained the highest values of chlorophyll-a and TSS. The characteristics of the spectra for the sample I4 agree with the physics of the situation, a high TSS concentration increases the radiance, and the high CDOM value for this sample decreases the radiance at wavelengths < 600 nm.

The next figures, 5.59, 5.60, and 5.61, plot the sensor-reaching radiances for various water types and bottom types at 0.5 m, 1 m, and 30 m respectively. In Figs. 5.59 and 5.60, the plots for each water type are grouped by color, based on bottom type, for legibility purposes. The 30 m plot does not show which bottom type the spectra represent.
because at 30 m, the water is deep enough that the bottom has no influence on the radiance. These spectra were used as the deep water data in the application of the algorithm to the HydroMod output.

Figure 5.59 Sensor-Reaching Radiances at Depth of 0.5 m

Figure 5.60 Sensor-Reaching Radiances at Depth of 1 m
Figure 5.61 Sensor-Reaching Radiances at Depth of 30 m

Aside from the radiances calculated for the HydroMod green algae bottom, the other radiances spectra are similar in shape. At one point, an area of the C9 Ginna image was selected, that was known to contain red rocks on the bottom, and a z-profile (where $z =$ wavelength) of the radiances spectra at each wavelength was collected using ENVI. Then, a crude procedure was implemented to try to match the shape of the z-profile to the shape of the radiances spectra output from the HydroMod runs. The z-profile matched to one of the Ontario sand spectra by minimizing the RMS error between the z-profile and the HydroMod radiances spectra. Several other areas in the image known contain some type of rock bottom matched to Ontario sand spectra as well. This seems to be because there is not a significant difference in the output spectra from HydroMod, especially in the 24 bands that were retained from the MISI image.
The principal components regression was attempted on the HydroMod outputs. The deep-water correction was performed by subtracting the 30 m spectra generated by HydroMod from the spectra generated for the other depths, and then taking the natural log of the result. The principal components analysis was then performed on the linearized data. Fig. 5.62 is the plot of the eigenvalues from the PCA.

![Eigenvalues from PC on Model](image)

**Figure 5.62 Eigenvalues from the PCA on Model Data**

The first principal component accounts for 80.5% of the variability in the data, the second for 11.3%, and the third for 3.5%. Depth accounts for 80% of the variability in the data. Next, the first three principal components were regressed against the inputs, depth, bottom type, and water type in order to obtain regression coefficients. The regression failed with regard to bottom type and water type because the inputs, numbers representing the bottom type or water type, had no physical meaning and regression does not work on categorical data. The regression predicted the depth with an RMS error of
0.82 m which is not very accurate because it is greater than one of the depths the regression is attempting to predict. The depth does not account for 100% of the variation in the data. The effects of depth, bottom type, and water type cannot be completely separated and still have some influence on one another even after principal components analysis.

The images of Ginna discussed in previous sections were transformed into Y and $Y_\perp$ using the algorithm and then the depth regression coefficients determined from the HydroMod model data were applied to see what depths would be predicted (Figs. 5.63-5.65). Then, these values were compared to actual ground truth.

![Image](image_url)

Figure 5.63 Quantitative Depth Results for Ginna_left
Figure 5.64 Quantitative Depth Results for Ginna_right

Figure 5.65 Quantitative Depth Results for Ginna_middle
Some fairly reasonable estimates were made of depth. However, there are some limitations to using the PCR for this application which will be discussed in the following chapter.
Chapter 6

Conclusion

Recently, increased attention has been given to studying shallow water to include the effects of bottom reflectance. Great potential exists for determining qualitative water depths and bottom type maps in the shallow coastal waters of Lake Ontario. The implementation of Philpot’s (1989) principal components algorithm was successful under certain conditions. The approach used in this research to determine quantitative depth and bottom type information had serious limitations, but introduced the concept of incorporating the radiative transfer model, HydroMod, into this type of bathymetric research.

Philpot’s method (1989) was chosen for implementation for a number of reasons. The first was ease of implementation. The algorithm consists mainly of a deep-water correction and principal components analysis (PCA), which was easy to implement because there are PCA programs available. The principal components algorithm was more flexible than other methods for bottom type mapping and water depth determination, because the main assumptions of Philpot’s algorithm (1989) are vertically homogeneous water and constant water type. In addition, the algorithm takes advantage of the hyperspectral nature of the MISI images upon which it was implemented. The algorithm was implemented in a variety of situations on a MISI image (C9) taken 3 September 1999 on a perpendicular flight path over the Ginna power plant. This
particular image was selected for its perpendicular nature because there were more deep-water areas than in the parallel-to-shore images. Another benefit of the perpendicular image is that the deep water can be selected from an area of the image that has the same ground instantaneous field of view as the shallow water area that is being processed. Therefore, the deep water contains the same atmospheric conditions and lighting conditions as the shallow water from which it is being subtracted, which is important since the angular effects were not taken into account. In addition to the image near the Ginna power plant, an image taken on 5 July 2000 near Ontario Beach was processed in order to analyze the potential of the algorithm for future algae distribution mapping.

First, the entire shallow area in the C9 image taken near Ginna was processed by selecting different areas of the image for deep water. The selection of deep water had a great impact on the results of the processing. Substantial non-linearities occurred when a deep water area included different water types. One example included selecting deep water over the entire width of the image. This particular image contained different water types that were visible from the image itself, as shown in the C9 image of Ginna (Fig. 6.1).
By selecting the deepwater pixels over the entire width of the image, part of the light water from the left side of the image was included. The same light water does not appear in the shallow water areas of the image. The qualitative depth and bottom type maps from this particular example (Fig. 6.2 and 6.3) are inaccurate.
The bottom type map shows none of the bottom type variations that were visible from the image itself. The interpretation of the depth map is that the water becomes deeper moving away from shore and then becomes shallow again nearing the left edge of the image, where the lighter water occurs. Better results are obtained by selecting deepwater pixels from the right side of the image where the water appears to be more consistent with the water over the shallow areas. The scatter plot is significantly more linear than the plot obtained from the previous example. However, though they were improved over the example using deepwater from the entire width of the image, the bottom type map and water depth map (Fig. 6.4 and 6.5) were still inaccurate.

Figure 6.4 $Y_{\parallel}$ using deep water from right
(-Depth)

Figure 6.5 $Y_{\perp}$ using deep water from right
(-Bottom Type)

The depth map still showed the trend of the water getting deeper and then shallower moving away from shore, which ground truth and bathymetry disproved.

The nonlinearities of the above examples result from the deepwater correction, because several pixels are averaged to form a single deep-water observation, used to
linearize the entire shallow-water image. If the deep-water pixels contain different water types and/or if the shallow-water image contains different water types, the deep-water correction will lead to errors caused by these different water types.

The algorithm is more successful over smaller sections of the image because there is typically less variation in smaller portions. When a shallow water area from the right side of C9 is processed with deep-water pixels from the same columns of the image, the results are very intuitive. The water increased in depth moving further away from shore (Fig.6.6). The bottom type map (Fig. 6.7) picked up on bottom type variations that were visible in the image itself, but the bottom maps are somewhat correlated with depth.

Two additional sections of the image were chosen for processing because the corresponding deep-water pixels appeared to be of the same water type. The shallow water images overlapped and the interesting feature was a “trench” that appeared in both

![Figure 6.6](image1.png)  ![Figure 6.7](image2.png)

Figure 6.6 $Y_{||}$ (~depth) for Ginna_right  Figure 6.7 $Y_{\perp}$ (~bottom type) for Ginna_right
of them. Some inaccuracies are still evident in these smaller images due to the presence of the lighter water and also variant lighting conditions.

The assumptions of the algorithm restrict its application to areas that contain invariant water type and atmospheric conditions. Another limitation involved in using the Case 2 assumptions (variable depth, variable bottom type, constant water type) is that the image must contain depth variation as well as bottom type variation. The images must be pre-processed to reduce noise effects, and as is evident in using the MISI images, the NIR bands may have to be deleted because they may contain mostly noise and very little signal. The NIR bands carry little information because these wavelengths do not penetrate very far into the water. The PCA picks up on any variation in the data; if there is significant noise, it becomes one of the main sources of variation. If the image contains land pixels, these must be masked out to eliminate land variability.

The flexibility and multiplicity of utilities that HydroMod has was demonstrated here. For a variety of bottom types, water types, and depths, water leaving radiances were generated for a particular atmosphere to be used as a calibration model for a Principal Components Regression. HydroMod radiance outputs matched expectations based on knowledge of the effect that aquatic component concentrations have on reflectance spectra. One of the September 3, 1999 Ginna water samples contained a relatively high amount of chlorophyll-a and total suspended solids, which could be seen in the spectrum of sensor-reaching radiances. The sample with high chlorophyll and TSS peaked in the green due to the chlorophyll and was significantly brighter than the other
spectra, which is characteristic when there is high TSS. This sample was collected from an area near the left side of the image, (Fig. 6.8), in the lighter water (A), which corresponds to the brighter spectra for this sample.

Figure 6.8 Smaller portion of Image C9 (Ginna)

For the 24 bands retained while working with the Ginna images, and also the HydroMod data, there was not significant difference between the shape of the spectra over the various bottom types, although there was some difference in magnitude. This is the reason why the z-profile method of verifying bottom type did not work. An area of the image that appeared to be a different bottom type was selected and then a z-profile of some of the pixels in that area were averaged and normalized. When all of the HydroMod spectra were normalized in an attempt to match the shape of the image z-profile to the normalized HydroMod spectra, the z-profile of the image bottom type consistently matched to Ontario sand. There was not enough variation in the spectra,
with the exception of HydroMod algae; however, there did not appear to be any areas in the image that consisted of HydroMod algae.

The Principal Components Regression approach to determining quantitative results from the algorithm had some success with the depth information, although there are serious limitations to this approach. PCR attempts to reduce the collinearity in the data, which is a problem for other linear regression models, by regressing the concentrations on the PCA scores as opposed to the constituent concentrations themselves. PCA can also have problems with collinearity, though, if the concentrations of two important constituents in the calibration samples are always present in the same ratio. The PCR was calibrated using the radiance outputs from HydroMod, for which the input “concentrations” of depth, water type, and bottom type were known. One limitation of this approach is that the model is scene-specific – the atmosphere, bottom types, and water types, are for a specific location and day. Another limitation is that determining the bottom types and water types for the scene is somewhat arbitrary. There are mixed bottom types at Ginna, containing some sand, some algae and some rock in mixed patches. It is difficult to model the radiance that comes from this mixture of bottom types.

The PCR on depth information resulted in a 0.82 m RMS error, which is not very accurate considering one of the inputs was 0.5 m. However, the depth estimates were somewhat consistent with the actual depths. The PCR on bottom type and water type information did not perform at all because regression does not work on categorical data,
which is grouped in categories with no ordinal significance. No information was
gathered from PCR on these two inputs; each bottom type and water type were simply
assigned a number to represent them, with no physical meaning to the number. More
work needs to be done in this area, looking at categorical data analysis, or perhaps
figuring out another way to relate categorical data to a principal component.

The eigenvector analysis on the model data showed that over 80% of the
variability in the data is contained in the first principal component, and therefore is due to
depth. Only 11.3% of the variability is due to bottom type. As discussed earlier, there
was not significant variability in the radiance spectra. This method would perhaps work
better in the Ontario Beach area where there are two bottom types that differ
significantly, algae (or the rock it grows on) and sand. Another consideration is how
many bands are retained; some of the bands that are deleted may contain most of the
variability between bottom types.

Another limitation of PCR is that there is no guarantee that the largest common
variations will be related to changes in the constituent concentrations (Galactic 2000).
PCR will suffer if the constituent concentrations are collinear, which can be avoided by
using many observations.

Regression coefficients for depth were obtained through PCR and applied to the
actual image data from the C9 image of Ginna. The results were reasonable, although the
approach is somewhat arbitrary. There is no indication of how many different bottom
types, water types, or depths are needed to adequately calibrate the regression.
Monroe county is interested in the location of benthic algae near Ontario Beach in an attempt to manage the problem of dead algae washing up in the recreational areas. Some preliminary analysis was done to see if Philpot's algorithm (1989) would be of use in addressing the problem. A July 5, 2000 image taken parallel to shore, near the Ontario Beach area, was processed with the algorithm. Only a small section of the image was used due to noise, missing lines, and sun glare that runs down the middle of the image. The image, C2 is shown in Figure 6.9.

![Figure 6.9 C2 - Image near Ontario Beach](image)

The results of this processing were very encouraging for future work in this geographic area of the lake. There are predominantly two bottom types in the area – sand and rock with some algae growing on it. There were "ridges" in the image that was processed, as evidenced by the depth map and confirmed with ground truth. Also, the ridges were alternating bottom types, according to the map created using the second eigenvector and confirmed by ground truth. One of the characteristics of this image is that bottom type and depth are correlated, where there is sand, the water is shallower, and vice versa. The
effects of illumination conditions affected the right side of the depth map, which indicated that the water was shallow at the furthest point from shore. This is due to the glint that is down the center of the image C2 (Fig. 6.9), evidenced in the brighter right side of this portion of the image. The deep water was selected from a different portion of image C2, that is at a different angle from the shallow portion of the image, but the angle effects have not been analyzed here. This is an area for future study especially if most of the images that are being worked with are parallel to shore.

Images that are perpendicular to shore, or at least taken at a higher altitude, are better because there are more deepwater pixels. Images taken perpendicular to shore can take advantage of having deepwater pixels at the same angle from nadir as the portion of the image that is of interest. More perpendicular flight lines need to be planned for data collections.

Further work needs to be performed in taking advantage of the HydroMod data. Both the inputs and outputs for various conditions are known. The capability of this approach to relate depth to the principal components using the HydroMod data should be considered at the Ontario Beach area where there are two distinct bottom types.

Implementing Philpot’s (1989) algorithm on MASI data was challenging, but under the proper conditions, it performed reasonably well in obtaining qualitative depth and bottom type information. There is definite promise in using this algorithm to process the Ontario Beach images to determine algae distributions in the area. HydroMod also has potential in this area; however, it needs to be developed further.
Works Cited


Galactic Industries Corp. “Principal Component Regression.”


Appendix A: MISI Information
Modular Imaging Spectrometer Instrument (MISI)

The Digital Imaging and Remote Sensing Group at RIT has constructed an imaging spectrometer called the Modular Imaging Spectrometer Instrument which is a line scanner with a 6" rotating mirror coupled to a Cassegrain telescope of focal ratio f/3.3. Two 0.5mm square silicon detectors (broad-band visible) and two 1.5mm fiber optics are placed at the primary focal plane to give a GIFOV of 0.3 m and 1.0 m respectively at 0.3 km of altitude. The fibers lead to two separate 36-channel spectrometers to cover the EM spectrum from 0.440μm to 1.020μm in 0.010μm spectral bands. A pyramid mirror diverts some photons from the primary focal plane to five HgCdTe detectors for the long-wave infrared region; secondary focal planes are available in the SWIR and MWIR for future use (Feng, 1995). An on-board calibration system consisting of two blackbodies for the LWIR and a tungsten source for the visible completes this imaging system for gathering absolute radiometrically calibrated data for remote sensing applications.

The system is designed to serve as:

- an airborne laboratory for earth observation research
- a high resolution under-flight system for high-altitude aircraft and satellite sensor performance evaluation
- a versatile data collection platform for acquiring imagery to be used in algorithm development and evaluation for reconnaissance and environmental application
- and as a survey instrument for demonstration and proof-of-concept studies of image analysis methods in areas such as energy conservation, water quality assessment, and hazardous waste site management

http://www.cis.rit.edu/research/dirs/research/misi.html
8/17/00
The MISI Optical System

The Spectral Calibration of MISI

The Thermal Calibration of MISI

Web Reference:


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First Line-Scan Image Taken by the Broad-Band Visible Detectors on the MISI of the Rochester Skyline (12/02/95).

First Line-Scan Image Taken by the Broad-Band Visible Detectors on the MISI of the RIT Dormitories (12/02/95).
The overall optical system with the various focal planes is shown in the figure. The 6-inch clear aperture scan mirror will spin at up to 40 revolutions per second and folds the image onto a second fold mirror which reflects the image into the Dall-Kirkham Cassegrainian-style telescope. The converging image is split onto four slightly off-axis (less than 2 degrees) focal planes by a four-sided pyramid mirror. The on-axis rays pass through a hole in the center of the pyramid mirror and are used to sample the visible/near-infrared EM region. Of the four off-axis focal planes, two are in the along-track scan direction (one fore and one aft of the primary optical axis) and two are in the cross-track direction (one leading, one lagging the primary optical axis). Presently, only the on-axis (VIS/NIR) and cross-track (long-wave infrared) focal planes are utilized. The along-track focal planes are intended for additional detector modules. The modular nature of the focal planes allow for easy addition of new detectors arrays or modification of the existing ones. The total field-of-view is 90 degrees (plus/minus 45 degrees) with calibration standards being viewed within every full rotation.
Spectral Calibration of MISI Spectrometer Channels

With hyperspectral imaging, the absolute spectral calibration is extremely important since the detector response function is convolved with the estimate of the radiance-at-the-sensor (during the inversion to reflectance process). The detector response function itself (for typical hyperspectral systems) is completely characterized by the center wavelength and FWHM (full width half-max) of the gaussian. Errors in center spectral wavelength because of poor spectral calibration technique can result in gross radiometric errors when performing analysis on spectral features of ground targets that require spectral match-up.

By illuminating a spectroradiometer with a stable spectral line source, such as Mercury or Argon lamp, the spectroradiometer can be spectrally calibrated to tolerances tighter than 0.1 nm. The spectroradiometer can then be used illuminate the hyperspectral sensor array with narrow bandwidth light to find the maximum spectral response point (center) and FWHM of the typically Gaussian detector response function. From a discrete, fine scan through the visible wavelengths, the detector response functions for each channel of the imaging spectrometer can be determined. This spectral scan can also be used to find cross-talk between spectral channels as well as determine if there is grating misalignment in the hyperspectral imager.

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Overhead view of absolute radiometric calibration set up.

A Mercury line source is used to calibrate the monochromator.
A broad-band source is then put through the monochromator (illumination with 2.5nm bandwidths of light), collimated (since the MISI optics are focused at infinity), and detected at the spectrometer focal plane.
Appendix B:
IDL Programs
PRO deepwater, deepwater_mean

; NAME:
;   deepwater
;
; PURPOSE:
;   Read in the area that has been selected as "deep water" from
;   the MISI image. It will average the pixels over each band in
;   the image, returning a vector.
;
; EXPLANATION:
;   Program called by runpca_ginna.pro for use in deepwater
;   subtraction
;
; CALLING SEQUENCE:
;   deepwater, deepwater_mean
;
; INPUT PARAMETERS
;   None. The deepwater_filename is hardcoded into this procedure.
;   MISI images must be read into an intarr() because they are
;   unsigned integer
;
; OUTPUT PARAMETERS
;   deepwater_mean = a 1 column by zsize vector which contains the
;   average of the pixels over each band
;
; NOTES:
;   Make sure that the deepwater_filename corresponds to the image
;   that is being processed with runpca_ginna.pro
;
; REVISION HISTORY:
;   Nikole Wilson November 1999

;Name of the deepwater file. Assumes file is BSQ and hardcoded

depwater_filename='dirs/home/nlw4923/C9/ginna_right_deep'

Dimensions of the deepwater image hardcoded
xsize=308.0 ; Number of columns in deepwater image
ysize=16.0 ; Number of rows in deepwater image
zsize=24.0 ; Number of bands

;Print size of deepwater image before read to check dimensions
print, "size of deepwater filename"
print, size(deepwater_filename)

;Reading in the deepwater image
deepwater_image = intarr(xsize, ysize, zsize)
   print, "size of deepwater image before read"
   print, size(deepwater_image)
openr,lun,deepwater_filename,/GET_LUN
readu,lun,deepwater_image
close,lun
Free_LUN,lun

;Print size of deepwater image after read
print, "size of deepwater image"
print, size(deepwater_image)
; Getting MISO image calibrated radiance values into uW/cm^2sr^-1nm^-1
; because these are the units on the HydroMod output
deepwater_image=temporary(deepwater_image)/100.0

; Setting up the array which will hold the average value in each of
; the z bands

deepwater_mean=fltarr(zsize)

for i=0,(zsize-1) do begin
    sum = total(deepwater_image[*,*,i])
    deepwater_mean[i]=sum/(xsize*ysize)
endfor

; Printing out the average of the deepwater image
print,'deepwater mean'
print,deepwater_mean
print,size(deepwater_mean)

deepwater_mean=transpose(temporary(deepwater_mean))
PRO runpca_ginna,shore_image,a,eigenval,percentages,x,final,yest

; NAME:
; runpca_ginna
;
; PURPOSE:
; Implements Philpot's principal components algorithm (1989) on a
; MISI image. Also applies the regression coefficients obtained
; through principal components regression on HydroMod model data
; in pcrtest.pro
;
; EXPLANATION:
; The pc scores are stored in the parameter, final
; which can be imported into ENVI. The first band in final
; corresponds to the data multiplied by the first eigenvector,
; which provides depth information. The second band in final
; corresponds to bottom type information.
;
; CALLING SEQUENCE:
; runpca_ginna, shore_image,a,eigenval,percentages,x,final,yest
;
; INPUT PARAMETERS:
; None. The shore_image is read into the procedure. It must be
; read into an intarr because the MISI data is in unsigned integer.
; The regression coefficient matrix, b, is also read in.
;
; OUTPUT PARAMETERS:
; shore_image: the MISI image being processed by the algorithm
; a = zsize by zsize matrix containing the eigenvectors
; eigenval = zsize element vector containing the sorted eigenvalues
; percentages = zsize element vector containing the cumulative
; percentage variances associated with the
; principal components
; x = xsize x ysize x zsize matrix of deepwater-corrected data
; final = xsize x ysize x zsize matrix of transformed data.
; Obtained by multiplying the matrix x by a. The first
; band is the matrix Y, which corresponds to depth
; information and is a qualitative depth map. The second
; band is the matrix Y^t, which corresponds to bottom type
; information and is a qualitative bottom type map
; yest = 1 x h vector of quantitative depth information obtained by
; applying the regression coefficients, b, to the first
; score (1st eigenvector x the data)
;
; NOTES: The land must be masked in shore_image and set to a value of
; -1 so the land pixels are not included in the principal
; components analysis. The radiance values in shore_image are
; changed from calibrated radiances to uW/cm^2sr^-1nm^-1
; so the image data is in the same units as the HydroMod output
;
; PROCEDURES CALLED:
; deepwater,astrolib,pca
;
; REVISION HISTORY:
; Nikole Wilson November 1999
; Added ability to process just the unmasked data N. Wilson Jun '00
; Algorithm taken from Philpot (1989)
; Call deepwater procedure to read in the deepwater average vector
deepwater, deepwater_image, deepwater_mean
deepwater_mean=transpose(temporary(deepwater_mean))

; Opening shore_image

shore_filename='/dirs/home/nlw4923/C9/ginna_right'
; Setting up array for shore image
xsize=308.0
ysize=284.0
zsize=24.0
; Reading bsq shore image into an array
shore_image=intarr(xsize,ysize,zsize)
    print, "size of shore image before read"
    print, size(shore_image)
    openr,lun,shore_filename,'/GET_LUN
    readu,lun,shore_image
    close,lun
    Free_LUN,lun

; Setting up shore image into a 2-d array with the pixels down the side
; and the bands across the top

  g=xsize*ysize
shore_image = reform(temporary(shore_image),g,zsize)
; Changing it to floating point data
shore_image=temporary(shore_image)*1.0
; Changing calibrated radiances into uW/cm^2sr^-1nm^-1
shore_image=temporary(shore_image)/100.0
; Assigning water pixels to matrix "values"
values=where(shore_image gt -.005,count); the mask value of -1 has been changed due to changing the units

; Setting up one band image with the mask values so the yest matrix determined near the end can be reformed into the original spatial information
one_band=shore_image(\star,\star,0)
values_one_band=where(one_band gt -0.005,values_count)

h=count/zsize ; determining the number of observations that are just water pixels for dimensioning purposes
print,'shore_image has been reformed into a 2d matrix'
print,
print,'Size of shore_image:'
print, size(shore_image)
values_array=shore_image(values)
print,'Size of values array:'
print, size(values_array)
; Reforming the water pixels into an array with h columns and zsize rows for the deepwater subtraction
values_array=reform(temporary(values_array),h,zsize)

; Setting up a unit vector as big as the shore image so I can multiply it by the deepwater mean in order to subtract the mean matrix from the shore image or vice versa if the mean matrix value is larger than the shore_image value
mean=fltarr(h,zsize)
temp=(replicate(1.0,h,1))
print,'unit vector has been set up'
print,size(mean)
mean=deepwater_mean##temp
print,'mean_matrix has been created'
print,size(mean)
print,size(shore_image)

;Deepwater subtraction

;Subtract mean_matrix from shore_image.
x=fltarr(h,zsize)
;for i=0L,(g-1) do begin
for i=0L,(h-1) do begin
  for j=0,(zsize-1) do begin
    if (values_array(i,j) gt mean(i,j)) $
    then x(i,j)=(values_array(i,j)-mean(i,j)) else $
    x(i,j)=(mean(i,j)-values_array(i,j))
  endfor
endfor
print,'just ran loop'
print,size(x)

;Take natural log of non-zero data
logx= x*1.0
templogx=alog(x(where(x ne 0)))
logx(where(logx ne 0))=templogx
print,'Performed natural log function'

data=fltarr(zsize,h)
data=transpose(logx)
print,'data'
print,size(data)

;Reshaping linearized data (X) into original size image
shore_image(values)=logx
x=reform(shore_image,xsize,ysize,zsize)

data=transpose(temporary(data))

;Calling astrolib procedure to run two procedures that are required
;for PCA.pro
astrolib
;Running PCA.pro,
PCA,data,eigenval,eigenvect,percentages,/covariance,/silent

plot,eigenval
a=eigenvect
scores=transpose(a)#data
shore_image(values)=scores
final=reform(shore_image,xsize,ysize,zsize)
scores=transpose(scores)
xforpcr=fltarr(2,63972)
xforpcr(0,*)=1.0
xforpcr(1,*)=scores(0,*)
b=fltarr(1,2)
fname='/dirs/home/nlw4923/C9/b'
openr,unit,fname,/get_lun
readf,unit,b
close,unit
free_lun,unit

yest=xforpcr##b
print,'size of yest:',size(yest)

print,'done'

end
PRO PCA, data, eigenval, eigenvect, percentages, proj_obj, proj_atr, $ 
    MATRIX=AM, TEXTOUT=textout, COVARIANCE=cov, SSQ=ssq, SILENT=silent 

; NAME: 
; PCA 
; PURPOSE: 
   Carry out a Principal Components Analysis (Karhunen-Loeve Transform) 
; EXPLANATION: 
   Results can be directed to the screen, a file, or output variables 
   See notes below for comparison with the intrinsic IDL function PCOMP. 
; CALLING SEQUENCE: 
   PCA, data, eigenval, eigenvect, percentages, proj_obj, proj_atr, 
       [MATRIX =, TEXTOUT = , /COVARIANCE, /SSQ, /SILENT ] 
; INPUT PARAMETERS: 
   data - 2-d data matrix, data(i,j) contains the jth attribute value 
       for the ith object in the sample. If N_OBJ is the 
       total number of objects (rows) in the sample, and N_ATTRIB is 
       the total number of attributes (columns) then data should be 
       dimensioned N_OBJ x N_ATTRIB. 
; OPTIONAL INPUT KEYWORD PARAMETERS: 
   /COVARIANCE - if this keyword is set, then the PCA will be carried out 
       on the covariance matrix (rare), the default is to use the 
       correlation matrix 
   /SILENT - If this keyword is set, then no output is printed 
   /SSQ - if this keyword is set, then the PCA will be carried out on 
       the sums-of-squares & cross-products matrix (rare) 
   TEXTOUT - Controls print output device, defaults to !TEXTOUT 
       textout=1 TERMINAL using /more option 
       textout=2 TERMINAL without /more option 
       textout=3 <program>.prt 
       textout=4 laser.tmp 
       textout=5 user must open file 
       textout = filename (default extension of .prt) 
; OPTIONAL OUTPUT PARAMETERS: 
   eigenval - N_ATTRIB element vector containing the sorted 
       eigenvalues 
   eigenvect - N_ATTRIB x N_ATTRIB matrix containing the 
       corresponding eigenvectors 
   percentages - N_ATTRIB element containing the cumulative 
       percentage variances associated with the principal components 
   proj_obj - N_OBJ by N_ATTRIB matrix containing the projections of 
       the objects on the principal components 
   proj_atr - N_ATTRIB by N_ATTRIB matrix containing the projections of 

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the attributes on the principal components

OPTIONAL OUTPUT PARAMETER
MATRIX = analysed matrix, either the covariance matrix if /COVARIANCE

is set, the "sum of squares and cross-products" matrix if
/SSQ is set, or the (by default) correlation matrix.

Matrix will have dimensions N_ATTRIB x N_ATTRIB

NOTES:
This procedure performs Principal Components Analysis (Karhunen-

Loeve Transform) according to the method described in "Multivariate


Keywords /COVARIANCE and /SSQ are mutually exclusive.

The printout contains only (at most) the first seven principle
eigenvectors. However, the output variables EIGENVECT contain
all the eigenvectors

Different authors scale the covariance matrix in different ways.
The eigenvalues output by PCA may have to be scaled by 1/N_OBJ or
1/(N_OBJ-1) to agree with other calculations when /COVAR is set.

PCA uses the non-standard system variables !TEXTOUT and
!TEXTUNIT.
These can be added to one's session using the procedure ASTROLIB.

The intrinsic IDL function PCOMP (introduced in V5.0) duplicates
most
most of the functionality of PCA, but uses different conventions
and

normalizations. Note the following:

(1) PCOMP requires a N_ATTRIB x N_OBJ input array; this is the
transpose
of what PCA expects
(2) PCA uses standardized variables; use /STANDARIZE keyword to
PCOMP
for a direct comparision.
(3) PCA (unlike PCOMP) normalizes the eigenvectors by the square
root
of the eigenvalues.
(4) PCA returns cumulative percentages; the VARIANCES keyword of
PCOMP
returns the variance in each variable

EXAMPLE:
Perform a PCA analysis on the covariance matrix of a data matrix,
and write the results to a file

IDL> PCA, data, /COVAR, t = 'pca.dat'

Perform a PCA analysis on the correlation matrix. Suppress all
printing, and save the eigenvectors and eigenvalues in output
variables
PROCEDURES CALLED:
TEXTOPEN, TEXTCLOSE

REVISION HISTORY:
Immanuel Freedman (after Murtagh F. and Heck A.).  December 1993
Wayne Landsman, modified I/O December 1993
Converted to IDL V5.0  W. Landsman  September 1997
Fix MATRIX output, remove GOTO statements  W. Landsman August 1998
Changed some index variable to type LONG  W. Landsman March 2000

On_Error, 2 ;return to user if error

Constants
TOLERANCE = 1.0E-5 ; are array elements near-zero?

Dispatch table
IF N_PARAMS() EQ 0 THEN BEGIN
print, 'Syntax - PCA, data, [eigenval, eigenvect, percentages, proj_obj, proj_atr,]
print, [MATRIX =, /COVARIANCE, /SSQ, /SILENT, TEXTOUT=]
RETURN
ENDIF

SZ = size(data)
if SZ[0] NE 2 THEN $
BEGIN
HELP, data
MESSAGE, 'ERROR - Data matrix is not two-dimensional'
ENDIF

Nobj = sz[1] & Mattr = sz[2] ; Number of objects and attributes

IF KEYWORD_SET(cov) THEN BEGIN
msg = 'Covariance matrix will be analyzed'
; form column-means
temp = replicate(1.0, Nobj)
column_mean = (temp # data)/Nobj
X = (data - temp # transpose(column_mean))
ENDIF ELSE $
IF KEYWORD_SET(ssq) THEN BEGIN
msg = 'Sum-of-squares & cross-products matrix will be analyzed'
X = data
ENDIF ELSE BEGIN
msg = 'Default: Correlation matrix will be analyzed'
; form column-means
temp = replicate(1.0, Nobj)
column_mean = (temp # data)/Nobj
X = (data - temp # transpose(column_mean))
S = sqrt(temp # (X*X)) & X = X/(temp # S)
\[
A = \text{transpose}(X) \# X
\]

if arg_present(AM) then AM = A

; Carry out eigenreduction

\[
\text{triq}, A, D, E \quad ; \text{D contains diagonal, E contains off-diagonal}
\]

\[
\text{triq}, D, E, A \quad ; \text{D contains the eigen-values, A(*,i) - vectors}
\]

; Use TOLERANCE to decide if eigenquantities are sufficiently near zero

index = where(abs(D) LE TOLERANCE*MAX(abs(D)),count)

if count NE 0 THEN D[index]=0

index = where(abs(A) LE TOLERANCE*MAX(abs(A)),count)

if count NE 0 THEN A[index]=0

\[
\text{index} = \text{sort}(D) \quad ; \text{Order by increasing eigenvalue}
\]

D = D[index] & E=E[index]

A = A[*,index]

; Eigenvalues expressed as percentage variance and ...

\[
W1 = 100.0 \times \text{reverse}(D) / \text{total}(D)
\]

;... Cumulative percentage variance

\[
C = \text{replicate}(1., \text{Mattr}, \text{Mattr})
\]

for j = 1L, Mattr-1 do C[0,j] = fltarr(j)

\[
W = C \# W1
\]

; Define returned parameters

\[
\text{eigenval} = \text{reverse}(D)
\]

\[
\text{eigenvect} = \text{reverse(\text{transpose}(A))}
\]

\[
\text{percentages} = W
\]

; Output eigen-values and -vectors

if not keyword_set(SILENT) then begin

; Open output file

\[
\text{if not keyword_set(TEXTOUT) then TEXTOUT = textout}
\]

\[
\text{textopen,'PCA', TEXTOUT = textout}
\]

\[
\text{printf,'!TEXTUNIT,'PCA: ' + systime()}
\]

\[
\text{sz1 = strtrim(Nobj,2) & sz2 = strtrim(Mattr,2)}
\]

\[
\text{printf,'!TEXTUNIT,'Data matrix has ' + sz1 + ' objects with up}
\]

to ' + $ + 

\[
\text{sz2 + ' attributes'}
\]

\[
\text{printf,'!TEXTUNIT, msg}
\]

\[
\text{printf,!TEXTUNIT, ' '}
\]

\[
\text{printf,!TEXTUNIT, ' '}
\]

\[
\text{printf,!TEXTUNIT, 'Eigenvectors As Percentages Cumul.'}
\]

\[
\text{percentages'}
\]

\[
\text{for i = 0L, Mattr-1 do $}
\]

\[
\text{printf,!TEXTUNIT, eigenval[i], W1[i], percentages[i] ,f =}
\]

\[
'(3f15.4)'
\]

\[
\text{printf,!TEXTUNIT, ''}
\]

\[
\text{printf,!TEXTUNIT, 'Corresponding eigenvectors follow...'}
\]

\[
\text{Mprint = Mattr < 7}
\]

\[
\text{header = ' VBLE '}
\]

\[
\text{for i = 1, Mprint do header = header + ' EV-' + strtrim(i,2) +}
\]

\[
\text{printf,!TEXTUNIT, header}
\]

\[
152
\]
for i = 1L, Mattr do printf,!TEXTUNIT, $ i, eigenvect[0:Mprint-1,i-1], f=(i4,7f9.4)

endif

; Obtain projection of row-point on principal axes (Murtagh & Heck
convention)
projx = X # A

; Use TOLERANCE again...
index = where(abs(projx) LE TOLERANCE*MAX(abs(projx)),count)
if count NE 0 THEN projx[index]=0
proj_obj = reverse( transpose(projx) )

if not keyword_set( SILENT ) then begin
    printf,!TEXTUNIT,' 
    printf,!TEXTUNIT, 'Projection of objects on principal axes ...
    printf,!TEXTUNIT,' 
    header = ' VBLE 
    for i = 1L, Mprint do header = header + ' PROJ- ' + strtrim(i,2) +

    printf,!TEXTUNIT, header
    for i = 0L, Nobj-1 do printf,!TEXTUNIT, $
        i+1, proj_obj[0:Mprint-1,i], f=(i4,7f9.4)
endif

; Obtain projection of column-points on principal axes
projy = transpose(projx)#X

; Use TOLERANCE again...
index = where(abs(projy) LE TOLERANCE*MAX(abs(projy)),count)
if count NE 0 THEN projy[index] = 0

; scale by square root of eigenvalues...
temp = replicate( 1.0, Mattr )
proj_atr = reverse(projy)/(sqrt(W)#temp)

if not keyword_set( SILENT ) then begin
    printf,!TEXTUNIT,' 
    printf,!TEXTUNIT, 'Projection of attributes on principal axes ...'

    printf,!TEXTUNIT,' 
    printf,!TEXTUNIT, header
    for i = 0L, Mattr-1 do printf,!TEXTUNIT, $
        i+1, proj_atr[0:Mprint-1,i], f=(i4,7f9.4)
endif

textclose, TEXTOUT = textout ; Close output file
RETURN
END
Appendix C: Standard Methods Chl-a process
I. Title: Chlorophyll a

II. Description:
Chlorophyll a constitutes approximately 1 to 2% of the dry weight of organic material in all planktonic algae and is the preferred indicator for algal biomass estimates.

Application: This method measures the amount of photosynthetic pigments in the water, both chlorophyll a, and its degradation product, pheophytin a. Interferences from less important pigments are corrected for by the use of several wavelengths.

Summary of Method: The sample is filtered to remove algae. The filter with the algae is then ground in aqueous acetone stored over MgCO₃ to extract the chlorophyll from the cells. The extract is centrifuged to remove the filter and cellular debris, and absorbance is read on a spectrophotometer. Four wavelengths are read. Each pigment absorbs at a particular wavelength, for example: chl. c absorbs at 630 nm, chl. b absorbs at 647 nm, chl. a absorbs at 664 nm and the turbidity blank is measured at 750 nm. The extract is then acidified so as to break down the chlorophyll a to pheophytin. Absorbance is read again. The absorbance values are then used in equations, which compensate for the various interferences, to obtain final results.

III. Reference

IV. Environmental Laboratory Approval Program (ELAP) Method code
none

V. Special Safety Precautions: See Material Safety Data Sheets (MSDS) for:
   a. acetone
   b. magnesium carbonate, MgCO₃
   c. hydrochloric acid, HCl, concentrated

VI. Precision Statement - based on 1996 data

<table>
<thead>
<tr>
<th>Range</th>
<th>Analyte</th>
<th>Mean</th>
<th>UWL</th>
<th>UCL</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;25 μg/L</td>
<td>Uncor. Chlor a</td>
<td>0.38</td>
<td>0.96</td>
<td>1.25</td>
</tr>
<tr>
<td></td>
<td>Cor. Chlor a</td>
<td>0.74</td>
<td>1.86</td>
<td>2.41</td>
</tr>
<tr>
<td></td>
<td>Pheophytin</td>
<td>0.79</td>
<td>1.99</td>
<td>2.59</td>
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<td>&gt;25 μg/L</td>
<td>Uncor. Chlor a</td>
<td>7.3</td>
<td>na</td>
<td>24</td>
</tr>
<tr>
<td></td>
<td>Cor. Chlor a</td>
<td>na</td>
<td>na</td>
<td>na</td>
</tr>
<tr>
<td></td>
<td>Pheophytin</td>
<td>na</td>
<td>na</td>
<td>na</td>
</tr>
</tbody>
</table>
VII. ACCURACY STATEMENT

no external standards are available for this analysis at this time

VIII. EQUIPMENT AND SUPPLIES

Note that all glassware must be acid-free

A. Spectrophotometer, with a narrow band resolution (0.5 to 2 nm) Use the Varian
DMS-90 UV-visible spectrophotometer.
B. Cuvettes - matched with 2 cm path length.
C. Tissue grinder, ground glass-ground glass - A.H.T. Co. #126
D. Centrifuge - use the DYNAC in the ME Lab.
E. Centrifuge tubes - 15ml glass - marked with line at 12 cm.
F. Corks - to stopper the centrifuge tube
G. Filtration equipment:
   1. Filter unit
   2. Membrane filters (Millipore brand) - 0.45 \( \mu \)m porosity, 47 mm diameter.
   3. Vacuum port with valve
H. Pasteur pipet with bulb
I. Automatic pipettor adjusted to deliver 2.80 ml
J. 1 ml graduated pipet with pipetting bulb
K. 250 ml graduated cylinder

IX. REAGENTS

A. Magnesium Carbonate Suspension 1%
   add 1.0 g finely powdered MgCO\(_3\) to 100 ml deionized distilled water. Stir well.
   Note: this will not go into solution.
B. Aqueous Acetone Solution, 90% (also known as 9+1)
   mix 900 ml acetone (reagent grade BP 56 c) with 100 ml deionized distilled water. (Final vol. will be less than 1000 ml).
C. 90% Acetone Containing Magnesium Carbonate Suspension
   mix 900 ml acetone with the above 100 ml of magnesium carbonate suspension
D. Hydrochloric acid, HCl, 1N
   Dilute 8.4 ml. concentrated HCl to 100 ml with deionized distilled water.
E. Hydrochloric acid, 0.1N
   Dilute 3 ml 1N HCl to 30 ml.

X. PRESERVATION AND HOLDING TIMES

1. Volume required: about 250 ml
2. Preservation:
   Filter within 24 hours, place filter with sample in a corked centrifuge tube. If the sample is then frozen and kept in the dark, it can be held up to 3 weeks.
XI. PROCEDURE

Note that Chlorophyll a is easily broken down by acids, light, and heat. All glassware should be acid-free, and samples should be processed away from excessive light and heat. Also samples should be covered to protect them from light when not being handled.

A. Filtration:

1. Shake sample to mix. Using the graduated cylinder, measure 250 ml of the sample.
2. Pour sample into the filtering unit with the filter in place and turn on the suction.
3. Rinse down the cylinder with the deionized distilled water and pour this into the filtering apparatus. Also rinse down the filter unit.
4. Remove the membrane filter from the filtering unit. Fold the filter 4 times and place into a centrifuge tube labeled w/the sample # and stopper with a cork.
5. If the extraction is to be done at a later date, freeze the filters in the tubes and keep in the dark. (i.e. wrap tubes in rack with aluminum foil and place in freezer).

B. Extraction:

1. Remove the filter from the centrifuge tube and place it inside the female half of the tissue grinder. Be sure filter falls all the way to the bottom of grinder. Do not use any acetone or start grinding until filter is in place.
2. Add 2 aliquots ~ 2.8 mls each of 90% acetone/ MgCO₃ using the automatic pipettor. (The MgCO₃ keeps the acetone basic and prevents the chlorophyll a from breaking down.)
3. Vortex on high to break up filter. Then, insert the male half of the tissue grinder, and proceed to grind the filter remnants until the sample is completely homogenized.
4. Lift the male half of the grinder, carefully, and rinse it into the female half with two aliquots 90% acet/susp., adding to extract.
5. Vortex to mix and pour the extract back into the centrifuge tube.
6. Add one aliquot ~ 2.8 mls of 90% acet./MgCO₃ using the automatic pipettor to the grinder.
7. Vortex to rinse and add rinse to centrifuge tube.
8. Using the pipettor, bring the volume in the centrifuge tube to 12 ml with 90% acet/susp.. Mix well with a Pasteur pipet. Cork.
9. Place each centrifuge tube in a rack in a covered container.
10. Repeat one in five samples and do two blanks. When all of the samples are done, place the tubes in the coldroom (4 °C) and steep for 24 hrs. in dark..

C. Analysis:

1. Remove rack from cold room and place tubes into white DYNAC centrifuge (in
ME area).

2. Set the timer for 30 min., and run centrifuge at full speed. (Speed should be increased in a couple of increments.)

3. Program the spectrophotometer (Varian DMS-90, UV/visible) according to #3.5 Multi wavelength operation pg. 15 in the Operation manual. Use 90% acetone in the 2 cm cells as blanks and program the spec. to read 630 nm, 645 nm, 664 nm, 665 nm, 750 nm. Zero the instrument at 630 nm. and check the zero at 647, 664 and 750. Subtract the slight reading for zero found at 750 nm from the sample's absorbance at 750 nm.

4. Remove the samples from the centrifuge and place into rack in the covered container.

5. Empty the cuvette to be used to read the samples, (the one at the front) and place it on a Kimwipe.

6. Wash Pasteur pipet proceed to pipette the sample into the cuvette, carefully so as not to disturb the sediment in the bottom of the centrifuge tube. Fill only to the stem leaving room for HCl addition later.

7. Place the cover on the cuvette, wipe faces with a clean Kimwipe, and check that they are clean. Then place cuvette in spectrophotometer.

8. Start the spectrophotometer running in multi mode and record readings at 630, 647, 664, and 750 nm.

9. Remove the cuvette and add 0.2 ml of 0.1 N HCL. Turn cuvette upside down 3X to mix the sample. Read the readings at 665, and 750 nm, after waiting at least 1 min. but no more than 2 minutes after adding the acid. Note: In multi mode the spectrophotometer pauses for 10 seconds after each wavelength. If you wait approx. 45 sec. after adding the acid then start the spec., the 665, 750 nm wavelengths will read between 1 min. 15 sec. and 1 min 35 sec.

10. Dump the sample into waste container for acetone.

11. Using the automatic pipettor fill cuvette halfway with 90% to rinse it, and dump into waste container.

12. Repeat steps #5 through #11 for each sample.

XII CALCULATIONS

Three parameters are determined:

A. Uncorrected chlorophyll a, this includes both chlorophyll a, and its degradation product pheophytin a but subtracts out chl b and c. (Trichromatic method.)

\[
a(\mu g/L) = \frac{11.85(OD_{660} - OD_{750}) - 1.54(OD_{647} - OD_{750}) - 0.08(OD_{647} - OD_{750}) \times ml \text{ extract} \times 10^3}{\text{ml sample} \times \text{cell path length cm.}}
\]

B. Corrected chlorophyll a
[26.73((OD₆₆₄-OD₇₅₀)-(OD₆₆₅ₐ-OD₇₅₀ₐ)) x ml extract x 10³]

CORR. a (µg/L) =  

X ml sample X cell path length cm.

C. PHEOPHYTIN a

[26.73(1.7(OD₆₆₅ₐ-OD₇₅₀ₐ)-(OD₆₆₄-OD₇₅₀)) x ml extract x 10³]

PHEO a (µg/L) =  

[ml sample x light path length cm]

Where a = reading after acidification

XII REPORTING

Detection limit is 0.1 µg/l.

<table>
<thead>
<tr>
<th>CONCENTRATION RANGE</th>
<th>REPORT TO NEAREST</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1 - 9.9 µg/l</td>
<td>0.1 µg/l</td>
</tr>
<tr>
<td>10 - 100 µg/l</td>
<td>1 µg/l</td>
</tr>
</tbody>
</table>

\[\text{Labchemwpdocs96chloro.txt}\]
Soak for 2 min in a second 100% propanol wash, filter, and add xylene. At least two washes are required; let the final one soak 10 min before filtering. Trim the xylene-soaked filter and place on a microscope slide on which there are several drops of mounting medium. Apply several more drops of medium to top of filter and install a cover glass. Carefully squeeze out excess mounting medium. Make the final mount permanent by lacquering the edges of the cover glass.

Count organisms using the most appropriate magnification. "Live" diatoms typically are red while "dead" ones are unstained. Oil immersion is necessary for species identifications of diatoms and many other algae. Count either strips or random fields and calculate plankton densities per milliliter:

\[
\text{No./mL} = \frac{C \times A_e}{A_e \times V}
\]

where:
- \(C\) = number of organisms counted,
- \(A_e\) = total area of effective filter before trimming and mounting.

† Permount, Fisher Scientific Co., or equivalent.

### 3. References


## 10200 G. Zooplankton Counting Techniques

### 1. Subsampling

Count entire samples having low zooplankton numbers (<200 zooplankters) without subsampling. However, most zooplankton samples will contain more organisms than can be enumerated practically; therefore, use a subsampling procedure. Before subsampling, remove and enumerate all large uncommon organisms such as fish larvae in fresh water or coelenterates, decapods, fish larvae, etc., in salt water. Subsample by the pipet or splitting method.

In the pipet method, adjust sample to a convenient volume in a graduated cylinder or Imhoff cone. Concentrating the plankton by using a rubber bulb and clear acrylic plastic tube with fine mesh netting fitted on the end is convenient and accurate (Figure 10200:9). For picoplankton and the smaller microzooplankton, use sedimentation techniques described for concentrating phytoplankton. Transfer sample to a beaker or other wide-mouth vessel for subsampling with a Hensen-Stempel or similar wide-bore pipet. Gently stir sample completely and randomly with the pipet and quickly withdraw 1 to 5 mL. Transfer to a suitable counting chamber.

Alternatively, subsample by splitting with any of a number of devices of which the Folsom plankton splitter is best known (Figure 10200:10). Level splitter before using. Place sample in the splitter and divide into subsplits. Rinse splitter into the subsamples. Repeat until a workable number (200 to 500 individuals) is obtained in a subsample. Exercise care to provide unbiased splits. Even when using the Folsom splitter unbiased subsamples cannot be unquestioningly assumed; therefore, count animals in several subsamples from the same sample to verify that the splitter is unbiased and to determine the sampling error introduced by using it.

Another method permits abundance estimates of more equivalent levels of precision among taxa than obtained with either the Hensen-Stempel pipet or the Folsom splitter. Normal counting procedures tally organisms on the basis of their abundance in a sample. Therefore, in a sample with a dominant organism making up 50% of total numbers, the tally of the dominant taxon will be large and have a small error. However, error about the subdominants will increase as the tally of each taxon decreases. By accepting one level of precision, the technique has been developed to obtain the same error about dominants and subdominants, permitting quantitative comparisons between taxa over successive times or between stations.

### 2. Enumeration

Using a compound microscope and a magnification of 100 x, enumerate small zoooplankton (protozoa, rotifers, and nauplii) in a 1- to 5-mL clear acrylic plastic counting cell fitted with a glass cover slip. For larger, mature microcrustacea use a counting chamber holding 5 to 10 mL. A Sedgewick-Rafter cell is not suitable because of size. An open counting chamber 80 by 50 mm and 2 mm deep is desirable; however, an open chamber is difficult to move without jarring and disrupting the count. A mild detergent solution placed on the chamber before counting reduces organism movements or special counting trays with parallel or circular grooves or partitions can be used. Count microcrustacea using a binocular dissecting microscope at 20 x to 40 x magnification. If identification is questionable, remove organisms with a microbiological transfer loop and examine at a higher magnification under a compound microscope.

Report smaller zooplankton as number per liter and larger forms as number per cubic meter:

\[
\text{No./m}^3 = \frac{C \times V'}{V' \times V''}
\]

\(A_e\) = area counted (strips or fields), and
\(V\) = volume of sample filtered, mL.
The concentration of photosynthetic pigments is used extensively to estimate phytoplankton biomass. All green plants contain chlorophyll a, which constitutes approximately 1 to 2% of the dry weight of planktonic algae. Other pigments that occur in phytoplankton include chlorophylls b and c, xanthophylls, phycobilins, and carotenes. The important chlorophyll degradation products found in the aquatic environment are the chlorophyllides, pheophorbid, and pheophytins. The presence or absence of the various photosynthetic pigments is used, among other features, to separate the major algal groups.

The three methods for determining chlorophyll a in phytoplankton are the spectrophotometric, the fluorometric, and the high-performance liquid chromatographic (HPLC) techniques. Fluorometry is more sensitive than spectrophotometry, requires less sample, and can be used for in-vivo measurements. These optical methods can significantly under- or overestimate chlorophyll a concentrations, in part because of the overlap of the absorption and fluorescence bands of co-occurring accessory pigments and chlorophyll degradation products.

Pheophorbide a and pheophytin a, two common degradation products of chlorophyll a, are also important in phytoplankton. Pheophorbide a is formed by the cleavage of the propionate side chain of chlorophyll a, while pheophytin a is formed by the removal of magnesium from chlorophyll a. These degradation products can be used as indicators of the degradation of chlorophyll a, and can provide insights into the dynamics of phytoplankton populations.

3. References

products of chlorophyll a, can interfere with the determination of chlorophyll a because they absorb light and fluoresce in the same region of the spectrum as does chlorophyll a. If these pheopigments are present, significant errors in chlorophyll a values will result. Pheopigments can be measured either by spectrophotometry or fluorometry, but in marine and freshwater environments the fluorometric method is unreliable when chlorophyll b co-occurs. Upon acidification of chlorophyll b, the resulting fluorescence emission of pheopigment b is coincident with that of pheophytin a, thus producing underestimation and overestimation of chlorophyll a and pheopigments, respectively.

HPLC is a useful method for quantifying photosynthetic pigments\textsuperscript{9,13,15,16,19-21} including chlorophyll a, accessory pigments (e.g., chlorophylls b and c), and chlorophyll degradation products (chlorophyllides, pheophorbides, and pheophytins). Pigment distribution is useful for quantitative assessment of phytoplankton community composition and zooplankton grazing activity.\textsuperscript{22}

1. Pigment Extraction

Conduct work with chlorophyll extracts in subdued light to avoid degradation. Use opaque containers or wrap with aluminum foil. The pigments are extracted from the plankton concentrate with aqueous acetone and the optical density (absorbance) of the extract is determined with a spectrophotometer. The ease with which the chlorophylls are removed from the cells varies considerably with different algae. To achieve consistent complete extraction of the pigments, disrupt the cells mechanically with a tissue grinder.

Glass fiber filters are preferred for removing algae from water. The filters assist in breaking the cells during grinding, larger volumes of water can be filtered, and no precipitate forms after acidification. Inert membrane filters such as polyester filters may be used where these factors are irrelevant.

- **Equipment and reagents:**
  1. **Tissue grinder:** Successfully macerating glass fiber filters in tissue grinders with grinding tube and pestle of conical design may be difficult. Preferably use round-bottom grinding tubes with a matching pestle having grooves in the TFE tip.
  2. **Clinical centrifuge.**
  3. **Centrifuge tubes,** 15-mL graduated, screw-cap.
  4. **Filtration equipment,** filters, glass fiber or membrane (0.45-μm porosity, 47-mm diam); vacuum pump; solvent-resistant disposable filter assembly, 1.0-μm pore size;\textsuperscript{3} 10-mL solvent-resistant syringe.
  5. **Saturated magnesium carbonate solution:** Add 1.0 g finely powdered MgCO\textsubscript{3} to 100 mL distilled water.
  6. **Aqueous acetone solution:** Mix 90 parts acetone (reagent-grade BP 56°C) with 10 parts saturated magnesium carbonate solution. For HPLC pigment analysis, mix 90 parts HPLC-grade acetone with 10 parts distilled water.

- **Extraction procedure:**
  1. Concentrate sample by centrifuging or filtering as soon as possible after collection. If processing must be delayed, hold samples on ice or at 4°C and protect from exposure to light. Use opaque bottles because even brief exposure to light during stor-

age will alter chlorophyll values. Samples on filters taken from water having pH 7 or higher may be placed in airtight plastic bags and stored frozen for 3 weeks. Samples from acidic water must be processed promptly to prevent chlorophyll degradation. Use glassware and cuvettes that are clean and acid-free.

- **Equipment and reagents:**
  1. **Spectrophotometer,** with a narrow band (pass) width (0.5 to 2.0 nm) because the chlorophyll absorption peak is relatively narrow. At a spectral band width of 20 nm the chlorophyll a concentration may be underestimated by as much as 40%.
  2. **Cuvettes,** with 1-, 4-, and 10-cm path lengths.
  3. **Pipets,** 0.1- and 1.0-mL.
  4. **Hydrochloric acid,** HCl, 0.1N.

- **Determination of chlorophyll a in the presence of pheophytin a:** Chlorophyll a may be overestimated by including pheopigments that absorb near the same wavelength as chlorophyll a. Addition of acid to chlorophyll a results in loss of the magnesium atom, converting it to pheophytin a. Acidify carefully to a final molarity of not more than 3 × 10\textsuperscript{-3}M to prevent certain accessory pigments from changing to absorb at the same wavelength as pheophytin a.\textsuperscript{13} When a solution of pure chlorophyll a is converted to pheophytin a by acidification, the absorption-peak ratio (OD\textsubscript{664}/OD\textsubscript{665}) of 1.70 is used in correcting the apparent chlorophyll a concentration for pheophytin a.

Samples with an OD\textsubscript{664} before/OD\textsubscript{665} after acidification ratio (664/665) of 1.70 are considered to contain no pheophytin a and to be in excellent physiological condition. Solutions of pure pheophytin show no reduction in OD\textsubscript{665} upon acidification and have a 664/665, ratio of 1.0. Thus, mixtures of chlorophyll a and pheophytin a have absorption peak ratios ranging between 1.0 and 1.7. These ratios are based on the use of 90% acetone as solvent. Using 100% acetone as solvent results in a chlorophyll a before-to-after acidification ratio of about 2.0.\textsuperscript{2}

Spectrophotometric procedure—Transfer 3 mL clarified extract to a 1-cm cuvette and read optical density (OD) at 750 and 664 nm. Acidify extract in the cuvette with 0.1 mL 0.1N HCl. Gently agitate the acidified extract and read OD at 750 and at 664 nm, 90 s after acidification. The volumes of extract and acid

---

\textsuperscript{1} Kontes Glass Co., Vineland, N.J. 08360: Glass/glass grinder, Model No. 8855; Glass/TFE grinder, Model 886000; or equivalent.

\textsuperscript{2} Whatman GF/F (0.7 μm), GF/A (1.0 μm), Gelman AE (1 μm),\textsuperscript{24} or equivalent.

\textsuperscript{3} Gelman Acrodisc or equivalent.
and the time after acidification are critical for accurate, consistent results.

The OD664 before acidification should be between 0.1 and 1.0. For very dilute extracts use cuvettes having a longer path length. If a larger cell is used, add a proportionately larger volume of acid. Correct OD obtained with larger cuvettes to 1 cm before making calculations.

Subtract the 750-nm OD value from the readings before (OD 664 nm) and after acidification (OD 665 nm).

Using the corrected values calculate chlorophyll a and pheophytin a per cubic meter as follows:

\[
\text{Chlorophyll } a, \text{ mg/m}^3 = \frac{26.7 \times (664_a - 665_a)}{V_1 \times L}
\]

\[
\text{Pheophytin } a, \text{ mg/m}^3 = \frac{26.7 \times [1.7 \times (665_a) - 664_a]}{V_2 \times L}
\]

where:

- \( V_1 \) = volume of extract, L
- \( V_2 \) = volume of sample, m³
- \( L \) = light path length or width of cuvette, cm.
- 664ₐ, 665ₐ = optical densities of 90% acetone extract before and after acidification, respectively.

The value 26.7 is the absorbance correction and equals \( A \times K \)

where:

- \( A \) = absorbance coefficient for chlorophyll \( a \) at 664 nm = 11.0, and
- \( K \) = ratio expressing correction for acidification.

\[
= \frac{(664_a) \text{ pure chlorophyll } a}{(665_a) \text{ pure chlorophyll } a - (664_a) \text{ pure pheophytin } a}
\]

\[
= \frac{1.7}{1.7 - 1.0} = 2.43
\]

c. Determination of chlorophyll \( a, b, \) and \( c \) (trichromatic method): Spectrophotometric procedure—Transfer extract to a 1-cm cuvette and measure optical density (OD) at 750, 664, 647, and 630 nm. Choose a cell path length or dilution to give OD664 between 0.1 and 1.0.

Use the optical density readings at 664, 647, and 630 nm to determine chlorophyll \( a, b, \) and \( c \), respectively. The OD reading at 750 nm is a correction for turbidity. Subtract this reading from each of the pigment OD values of the other wavelengths before using them in the equations below. Because the OD of the extract at 750 nm is very sensitive to changes in the acetone-to-water proportions, adhere closely to the 90 parts acetone:10 parts water (v/v) formula for pigment extraction. Turbidity can be removed easily by filtration through a disposable, solvent-resistant filter attached to a syringe or by centrifuging for 20 min at 500 g.

Calculate the concentrations of chlorophyll \( a, b, \) and \( c \) in the extract by inserting the corrected optical densities in following equations:

\[
\begin{align*}
\text{a. } & C_a = 11.85(\text{OD664}) - 1.54(\text{OD647}) - 0.08(\text{OD630}) \\
\text{b. } & C_b = 21.03(\text{OD647}) - 5.43(\text{OD664}) - 2.66(\text{OD630}) \\
\text{c. } & C_c = 24.52(\text{OD630}) - 7.60(\text{OD647}) - 1.67(\text{OD664})
\end{align*}
\]

where:

- \( C_a, C_b, \) and \( C_c \) = concentrations of chlorophyll \( a, b, \) and \( c \), respectively, mg/L, and
- OD664, OD647, and OD630 = corrected optical densities (with a 1-cm light path) at the respective wavelengths.

After determining the concentration of pigment in the extract, calculate the amount of pigment per unit volume as follows:

\[
\text{Chlorophyll } a, \text{ mg/m}^3 = \frac{C_a \times \text{extract volume, L}}{\text{volume of sample, m}^3}
\]

3. Fluorometric Determination of Chlorophyll \( a \)

The fluorometric method for chlorophyll \( a \) is more sensitive than the spectrophotometric method and thus smaller samples can be used. Calibrate the fluorometer spectrophotometrically with a sample from the same source to achieve acceptable results. Optimum sensitivity for chlorophyll \( a \) extract measurements is obtained at an excitation wavelength of 430 nm and an emission wavelength of 663 nm. A method for continuous measurement of chlorophyll \( a \) in vivo is available, but is reported to be less efficient than the in-vitro method given here, yielding about one-tenth as much fluorescence per unit weight as the same amount in solution. Pheophytin \( a \) can also be determined fluorometrically.

a. Equipment and reagents: In addition to those listed under 1a and 2a above:

- Fluorometer, \( \| \) equipped with a high-intensity F4T.5 blue lamp, photomultiplier tube R-446 (red-sensitive), sliding window orifices \( 1 \times, 3 \times, 10 \times \), and filters for light emission (CS-2-64) and excitation (CS-5-60). A high-sensitivity door is preferable.

- b. Extraction procedure: Prepare sample as directed in 1b above.

1) Calibrate fluorometer with a chlorophyll solution of known concentration as follows: Prepare chlorophyll extract and analyze spectrophotometrically. Prepare serial dilutions of the extract to provide concentrations of approximately 2, 6, 20, and 60 \( \mu \)g chlorophyll \( a/L \). Make fluorometric readings for each solution at each sensitivity setting (sliding window orifice): \( 1 \times, 3 \times, 10 \times \), and \( 30 \times \). Using the values obtained, derive calibration factors to convert fluorometric readings in each sensitivity level to concentrations of chlorophyll \( a \), as follows:

\[
F_x = \frac{C_x}{R_x}
\]

where:

- \( F_x \) = calibration factor for sensitivity setting \( x \)
- \( R_x \) = fluorometer reading for sensitivity setting \( x \)
- \( C_x \) = concentration of chlorophyll \( a \) determined spectrophotometrically, \( \mu \)g/L.

2) Measure sample fluorescence at sensitivity settings that will provide a mid-scale reading. (Avoid using the \( 1 \times \) window because of quenching effects.) Convert fluorescence readings to concentrations of chlorophyll \( a \) by multiplying the readings by the appropriate calibration factor.

---

\( \| \) Model 10-005, Turner Designs, Sunnyvale, Calif. or equivalent.
c. Determination of chlorophyll a in the presence of pheophytin a. This method normally is not applicable to freshwater samples. See discussion under 10200G and 1c above.

1) Equipment and reagents—In addition to those listed under 1a and 2a above, pure chlorophyll a# (or a plankton chlorophyll extract with a spectrophotometric before-and-after acidification ratio of 1.70 containing no chlorophyll b).

2) Fluorometric procedure—Calibrate fluorometer as directed in § 36). Determine extract fluorescence at each sensitivity setting before and after acidification. Calculate calibration factors $(F_r)$ and before-and-after acidification fluorescence ratio by dividing fluorescence readings obtained before acidification by the reading obtained after acidification. Avoid readings on the $1x$ scale and those outside the range of 20 to 80 fluorometric units.

3) Calculations—Determine the “corrected” chlorophyll a and pheophytin a in sample extracts with the following equations:8,24

\[
\text{Chlorophyll a, mg/m}^3 = F_r \left( \frac{R_a - R_b}{V_e} \right) V_e
\]

\[
\text{Pheophytin a, mg/m}^3 = F_r \left( \frac{R_a - R_b}{V_e} \right) V_e
\]

where:

$F_r$ = conversion factor for sensitivity setting $S$ (see § 2b, above),

$R_a$ = fluorescence of extract before acidification,

$R_b$ = fluorescence of extract after acidification,

$r = R_a/R_b$, as determined with pure chlorophyll a for the instrument (redetermine $r$ and $F_r$ if filters or light source are changed),

$V_e$ = volume of extract, and

$V_s$ = volume of sample.

d. Extraction of whole water, nonfiltered samples: Alternatively, to prevent cell lysis during filtration, extract whole water sample.

1) Equipment and reagents—Fluorometer equipped with a high-sensitivity R928 phototube** with output impedance of 36 mW at 675 nm and a high-sensitivity door. Place neutral density filter (40–60%) in the rear light path,†† selected to permit reagent blanking on the highest sensitivity scale.

2) Extraction procedure—Decant 1.5 mL sample into screw-cap test tube and add 8.5 mL 100% acetone. Mix with vortex mixer and hold in the dark for 6 h at room temperature. Filter through glass fiber filter†† or centrifuge. Measure fluorescence as described in Section 10200H.3 and estimate concentrations as in § 3c. Because humic substances interfere, if they are present filter a sample portion (see 10200H.16) and process filtrate with sample. Subtract filtrate (blank) fluorescence from that of sample.

d. High-Performance Liquid Chromatographic Determination of Algal Chlorophylls and Their Degradation Products

a. Equipment and reagents: In addition to those listed for pigment extraction, § 1a above:

1) High-pressure liquid chromatograph capable of a flow rate of 2.0 mL/min.

2) High-pressure injector valve equipped with a 100-μL sample loop.

# Purified chlorophyll a, Sigma Chemical Company, St. Louis, Mo., or equivalent.
** Hamamatsu Corp., Middlesex, N.J., or equivalent.
†† If using Model 10-005, Turner Designs, or equivalent.
## Whatman GF/F or equivalent.

3) Guard column (4.0 x 0.5 cm, C$_18$ packing material, 3-μm particle size, or equivalent protection system) for extending life of primary column.

4) Reverse-phase HPLC column.$§$

5) Fluorescence detector capable of excitation at 430 ± 30 nm and measuring emission at wavelengths greater than 600 nm.

6) Data recorder device: Strip chart recorder or, preferably, an electronic integrator.

7) Syringe, glass, 250-μL.

8) HPLC eluents: System A (80:1.5:5; methanol:Type I reagent water:ion-pairing solution) and System B (80:20; methanol:acetone). Use HPLC-grade solvents; measure volumes before mixing. Filter eluents through a solvent-resistant 0.45-μm filter before use and degas with helium. Prepare the ion-pairing (IP) solution from 15 g tetrabutylammonium acetate|| and 77 g ammonium acetate## made up to 1 L with Type I reagent water.15

9) Calibration standards: Individually dissolve 1 mg each pure chlorophyll a and b|| in 100 mL 90% acetone. Determine the exact concentrations spectrophotometrically (ε$_{664}$) for chlorophyll a in 90% acetone = 87.67 L g$^{-1}$ cm$^{-1}$, ε$_{664}$ for chlorophyll b in 90% acetone = 51.36 L g$^{-1}$ cm$^{-1}$). Prepare pheophytin a + a' and b + b' standards from the primary chlorophyll a and b standards by acidification with hydrochloric acid; correct respective concentrations for Mg$^{2+}$ loss. Extract chlorophyll c with 90% acetone from diatoms, purify by thin-layer chromatography (TLC)25 and calibrate spectrophotometrically (ε$_{664}$) and the exact concentrations spectrophotometrically (ε$_{664}$ for chlorophyll a = 128 L g$^{-1}$ cm$^{-1}$). Prepare pheophorbide a by acidification of chlorophyll a, purify by TLC,25 and calibrate spectrophotometrically in 90% acetone (ε$_{664}$ for pheophorbide a = 69.8 L g$^{-1}$ cm$^{-1}$). Standards stored under nitrogen in the dark at −20°C are stable for about 1 month.

b. Procedure:

1) Set up and equilibrate the HPLC system with solvent System A at a flow rate of 2 mL/min. Adjust fluorometer sensitivity to provide full-scale reading with the most concentrated chlorophyll a standard.

2) Calibrate HPLC system by preparing working standards from the primary standards (on day of use). Once retention times of the standards are determined for a particular system, simplify standardization by preparing serial dilutions from mixed standards. Prepare separately mixed standards for the chlorophylls and chlorophyllide a and for the pheophytins and pheophorbide a. Mix 1-mL portions of standards with 300 μL ion-pairing solutions and equilibrate for 5 min before injection (use of ion-pairing agents greatly enhances separation of depolytigated pigments, chlorophyllide a, chlorophyll c, and pheophorbide a). Prepare blanks by mixing 1 mL 90% acetone with 300 μL IP solution. Rinse syringe twice with 150 μL standard and draw

##§§ Microsorb C$_18$ column, 10 cm long, 3-μm particle size, Rainin Co., or equivalent.
##|| Fluka Chemical Corp., 980 South Second Street, Ronkonkoma, N.Y., or equivalent.
#### Sigma Chemical Company, or equivalent.
about 250 μL, standard into syringe for injection. Place syringe in injector valve, overfilling the 100-μL sample loop. Construct calibration curves by plotting fluorescence peak areas (or heights) against standard pigment concentrations.

3) Prepare samples for injection by mixing a 1-mL portion of the 90% acetone pigment extract with 300 μL IP solution.

4) Use a two-step solvent program to optimize separation of the chlorophylls from their degradation products. After injection, change from solvent System A to System B over 5 min and follow with System B for 15 min at a flow rate of 2 mL/min. Re-equilibrate the column with System A for 5 min before the next injection for a total analysis time of approximately 25 min. Degas the solvent systems with helium during analysis. Increase lifetime of HPLC column by storing it in 100% methanol between runs. Periodically flush the HPLC system with reagent water (Type I) to avoid buildup of ion pairing agents.

5) Calculate individual pigment concentrations using the following formula:

\[
C_i = \frac{A_i F V_i}{V_s} \]

where:

- \( C_i \): individual pigment concentration, mg/L,
- \( A_i \): area of individual pigment peak from sample injection,
- \( F \): standard response factor (μg pigment/0.1 mL standard divided by corresponding peak area),
- \( V_i \): injection volume (0.1 mL),
- \( V_e \): extraction volume, mL, and
- \( V_s \): sample volume, L.

6) This method is designed only for quantification of chlorophylls and their degradation products. Detect carotenoid pigments, which are also present in 90% acetone extracts but do not fluoresce, by absorbance spectroscopy (at about 440 nm).

7) The elution order and approximate retention times for the major chlorophyll pigments and their degradation products are shown in Figure 10200:11. The detection limits (s/n = 2) vary with fluorometer configuration and flow rate; however, they range from 10 to 100 pg per injection for most chlorophylls and their degradation products. The accuracy of the HPLC method depends primarily on purity of pigment standards. Preferably measure absorption spectra (350 to 750 nm) of the standards and compare with published data. Pigment purity also can be assessed by HPLC analysis, providing there are no co-eluting contaminants with absorption and fluorescence bands overlapping those of the standards. HPLC and spectrophotometrically derived pigment concentrations for available EPA standards agree reasonably well (±20%) if spectrophotometric results are corrected for the presence of pheopigments and the HPLC results are expressed as pigment equivalents (e.g., chlorophyll a equivalents = chlorophyllide a + chlorophyll a + chlorophyll a′, provided that the proper molecular weight corrections are applied). Thus, if significant amounts of chlorophyll derivatives are present, pigment concentrations determined spectrophotometrically will be over-estimated. The agreement between HPLC and spectrophotometrically derived results depends on the presence of accessory chlorophylls, \( b, c \), and their derivatives. Triplicate injections of a fivefold dilution of an EPA standard gave coefficients of variation of 7.5% (chlorophyllide a), 9.1% (chlorophyll c), 13.4% (pheophorbide a), 9.6% (chlorophyll b), 0.5% (chlorophyll a), 6.3% (pheophytin a), and 22.9% (pheophytin a′), with an average value of 10% for the seven pigments analyzed.

5. High-Performance Liquid Chromatographic Determination of Algal Chlorophyll and Carotenoid Pigments (PROPOSED)

\( \text{a. Equipment and reagents:} \) In addition to those listed for pigment extraction, \( ^\circ \) 1a above:

1) High-performance liquid chromatographic pump capable of gradient delivery of three different solvents at a flow rate of 1 mL/min.

2) High-pressure injector valve equipped with a 200-μL sample loop.

3) Guard column (50 × 4.6 mm, C18 packing material, 3-5 μm particle size) for extending life of primary column.

4) Reverse-phase HPLC column with endcapping (250 × 4.6 mm, 5-μm particle size, C18 column).***

5) Variable wavelength or filter absorbance detector with low-volume flowthrough cell. Detection wavelength is 436 nm.

6) Data recording device: Strip chart recorder or, preferably, an electronic integrator or computer equipped with hardware and software for chromatographic data analysis.

7) Syringe, glass, 500-μL.

8) HPLC eluents: Eluent A (80:20, v/v; methanol:0.5M ammonium acetate, pH 7.2); Eluent B (90:10, v/v; acetonitrile:water), and Eluent C, ethyl acetate. Use HPLC-grade solvents. Measure volumes before mixing. Filter eluents through a solvent-resistant 0.4-μm filter before use and degas with helium.

9) Calibration standards: Chlorophylls a and b, and \( \beta \)-carotene can be purchased as can zeaxanthin and lutein. Other pigment standards can be purified from plant extracts by

---

* Spherisorb ODS-2, Phase Separations Inc., Norwalk, Conn., or equivalent.
†† Sigma Chemical Co., St. Louis, Mo., or equivalent.
††† Roth Chemical Co., distributed by Atomergic Chemicals Corp., Farmingdale, N.Y., or equivalent.
Appendix D:
Processing Results for September 3, 1999
Results for September 3, 1999

Chlorophyll-a values were determined both spectrophotometrically and fluorimetrically.

The spectrophotometric results for Sep 3 are shown in Table D.1. The equations for converting the absorbance readings to concentrations are located in the Appendix C: Standard Methods.

Table D.1 September 3, 1999 Chlorophyll-a concentrations – determined spectrophotometrically

Chlorophyll-a results were also determined fluorimetrically. The excitation bandpass was set at 20 nm in order to have a lot of signal and the data values were recorded at an
emission bandpass of 5 nm for a higher resolution. The concentrations were determined using a standard chlorophyll solution to calibrate the data values to concentrations. The fluorimetrically determined chlorophyll-a values are shown in Table D.2.

<table>
<thead>
<tr>
<th>Sample #</th>
<th>Samp Vol (ml)</th>
<th>Xtr Vol (ml)</th>
<th>Data Value (20/5)</th>
<th>Conc (ug/L)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A3</td>
<td>600</td>
<td>10</td>
<td>42.61</td>
<td>1.49135</td>
</tr>
<tr>
<td>I1</td>
<td>600</td>
<td>10</td>
<td>21.94</td>
<td>0.7679</td>
</tr>
<tr>
<td>A2</td>
<td>600</td>
<td>10</td>
<td>50.09</td>
<td>1.75315</td>
</tr>
<tr>
<td>I4</td>
<td>750</td>
<td>10</td>
<td>102.26</td>
<td>2.86328</td>
</tr>
<tr>
<td>A6</td>
<td>800</td>
<td>10</td>
<td>58</td>
<td>1.5225</td>
</tr>
<tr>
<td>A5</td>
<td>800</td>
<td>10</td>
<td>38.53</td>
<td>1.011413</td>
</tr>
</tbody>
</table>

Table D.2 September 3, 1999 Chlorophyll-a values determined fluorimetrically

The TSS values were also calculated for each of the water samples and are shown in Table D.3:

<table>
<thead>
<tr>
<th>Filter #</th>
<th>Sample #</th>
<th>Vol Filtered (ml)</th>
<th>Pre-weight (g)</th>
<th>Post-weight (g)</th>
<th>Difference</th>
<th>TSS (mg/L)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>A3</td>
<td>600</td>
<td>0.0351</td>
<td>0.0359</td>
<td>0.0008</td>
<td>1.333333</td>
</tr>
<tr>
<td>2</td>
<td>I1</td>
<td>600</td>
<td>0.0354</td>
<td>0.0360</td>
<td>0.0006</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>A2</td>
<td>600</td>
<td>0.0361</td>
<td>0.0367</td>
<td>0.0006</td>
<td>1</td>
</tr>
<tr>
<td>4</td>
<td>I4</td>
<td>750</td>
<td>0.0365</td>
<td>0.0383</td>
<td>0.0018</td>
<td>2.4</td>
</tr>
<tr>
<td>5</td>
<td>A6</td>
<td>800</td>
<td>0.0366</td>
<td>0.0372</td>
<td>0.0006</td>
<td>0.75</td>
</tr>
<tr>
<td>6</td>
<td>A5</td>
<td>800</td>
<td>0.0357</td>
<td>0.0365</td>
<td>0.0008</td>
<td>1</td>
</tr>
</tbody>
</table>

Table D.3 September 3, 1999 TSS Values

The CDOM scalar values were obtained from another student who performed the processing. These values are located in Table D.4.
As a verification of my chlorophyll-a processing, three filters from the July 26, 1999 collect were delivered to the County Health Lab for processing. The results of the comparison are shown below in Table D.5. The County Health Lab chemists process chlorophyll samples on a weekly basis and felt that the outcome of the comparison indicates that our processes yield comparable results. Further development of a control is necessary to test the robustness of the RIT chlorophyll processing procedure, to include sending more samples to the Health Lab and testing to see how the presence of chlorophyll degrades over storage time.

Table D.5 Comparison of Chlorophyll-a processing results
Some of the discrepancies between the values determined by the County and RIT can be attributed to instrumentation and slight differences in processing. The spectrophotometer in the basement would not stay "zeroed". After the blank acetone sample was zeroed, the reading on the blank fluctuated between −0.001 and −0.003 regardless of the number of times the blank sample was zeroed. The County Health Lab uses a Teflon tip on a drill to grind the glass filters. The grinders at RIT were glass and the glass filters tend to wear down the grinding texture of the pestel, decreasing its effectiveness in grinding. At times, the Health Lab uses filters that are larger in size and are not made of glass. These slight differences may account for some of the discrepancies.